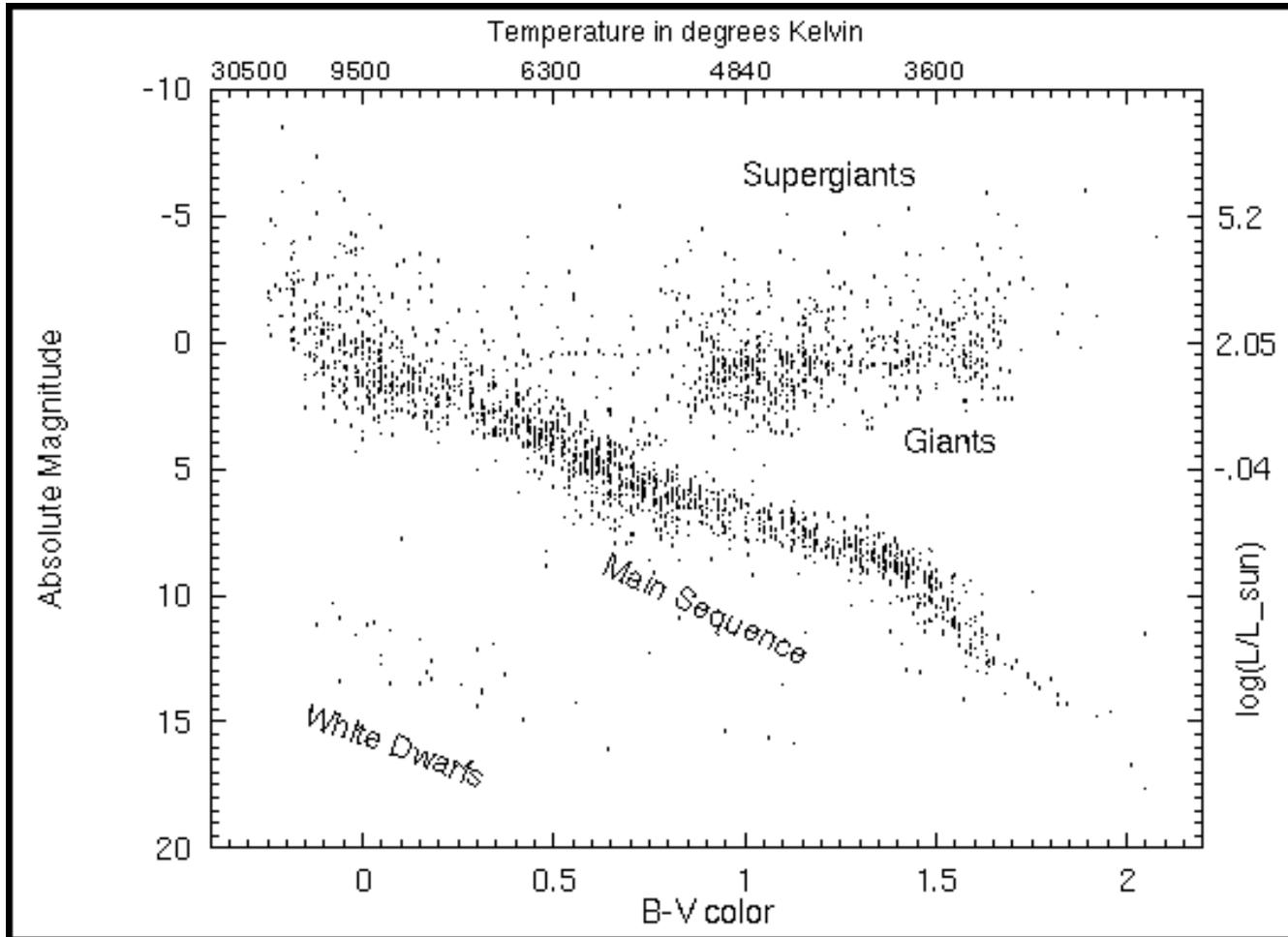
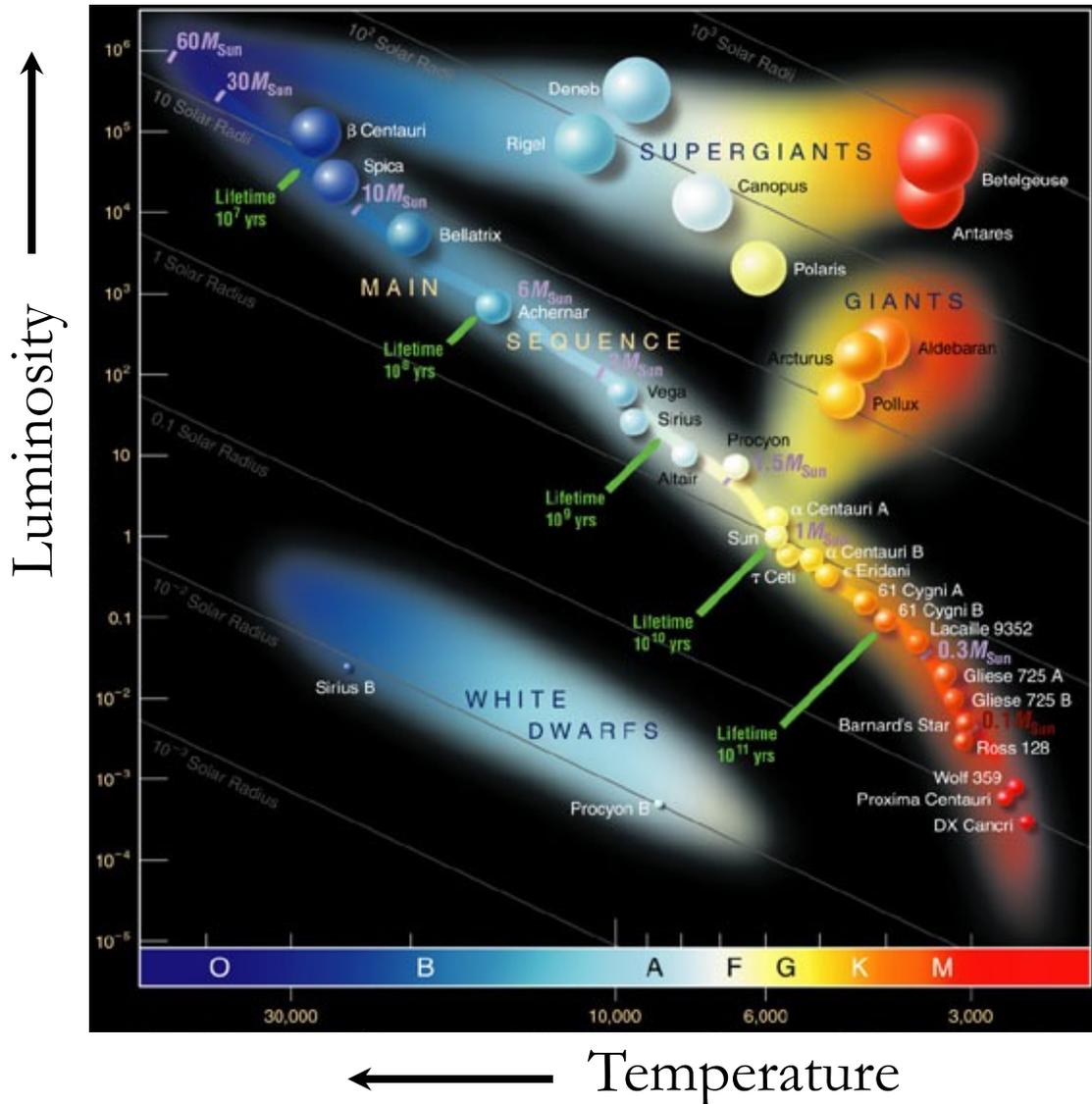


Lecture 15

The Hertzsprung–Russell diagram

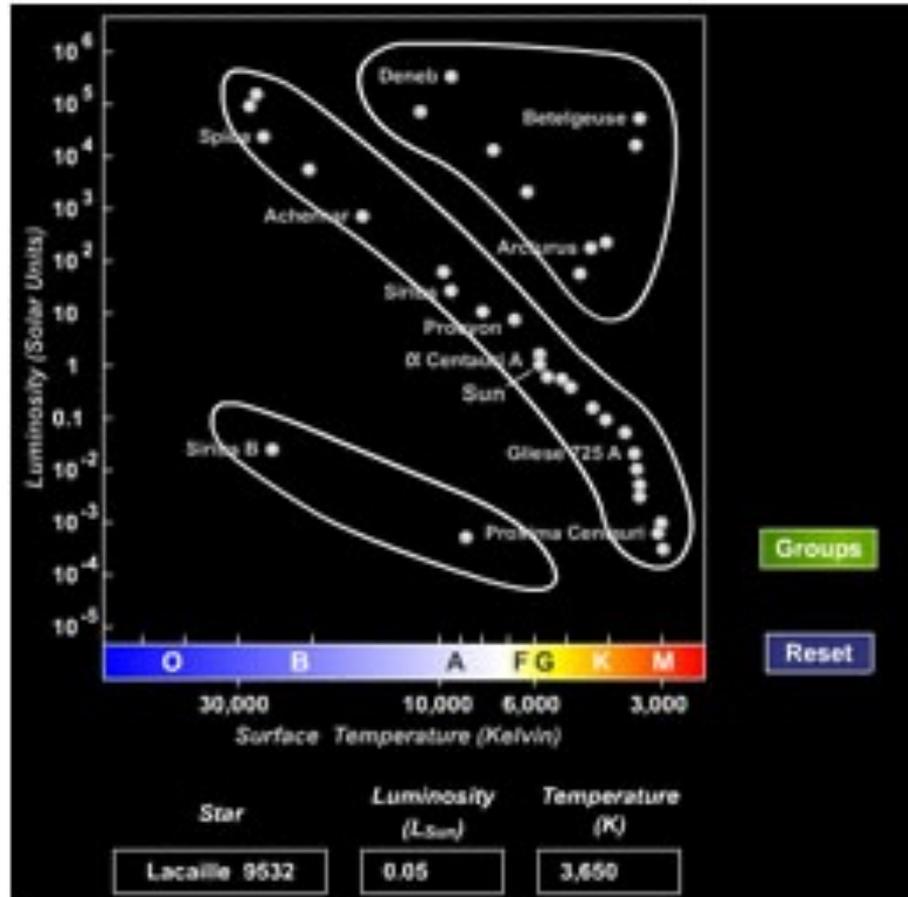


The Hertzsprung–Russell diagram

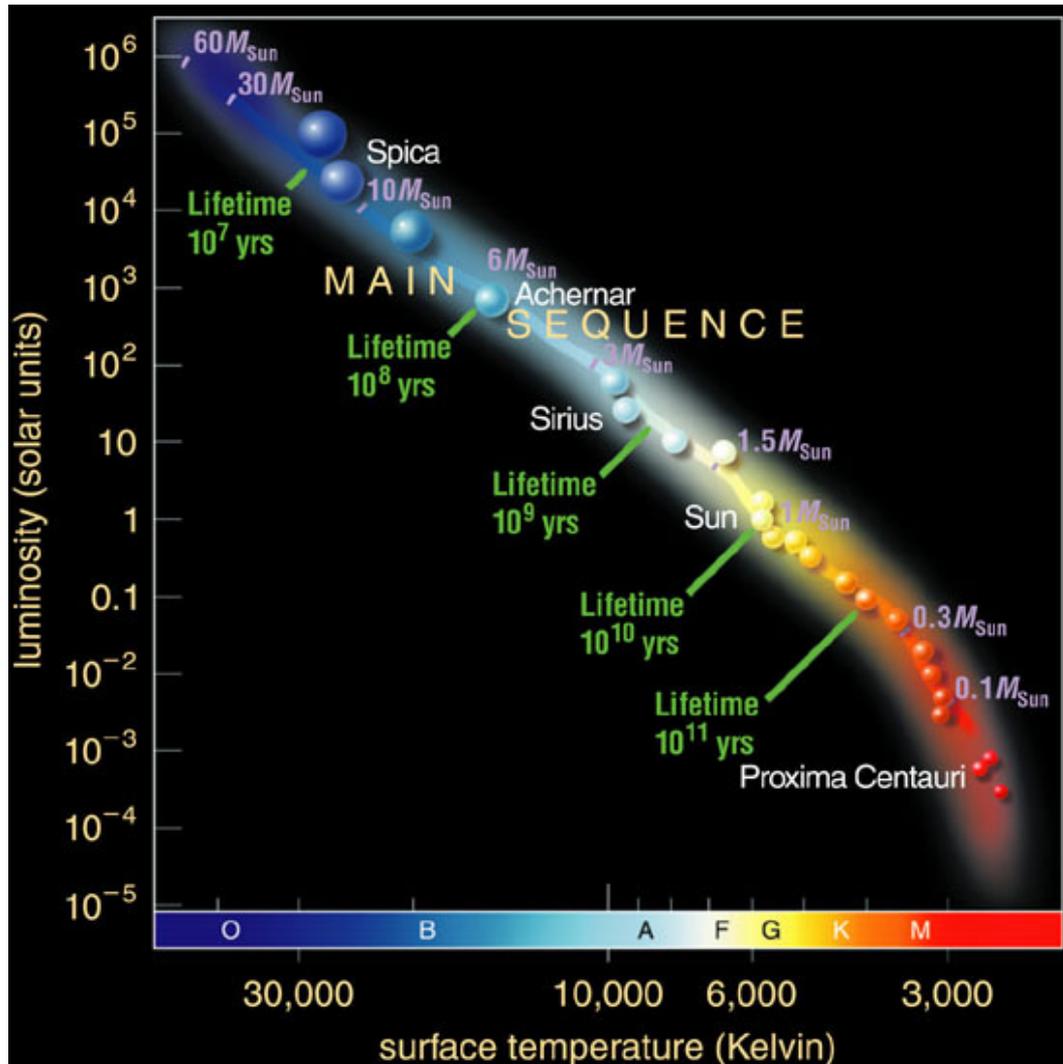


An H-R diagram plots *properties* of stars: the **luminosities** versus **temperatures**.

The Hertzsprung–Russell diagram

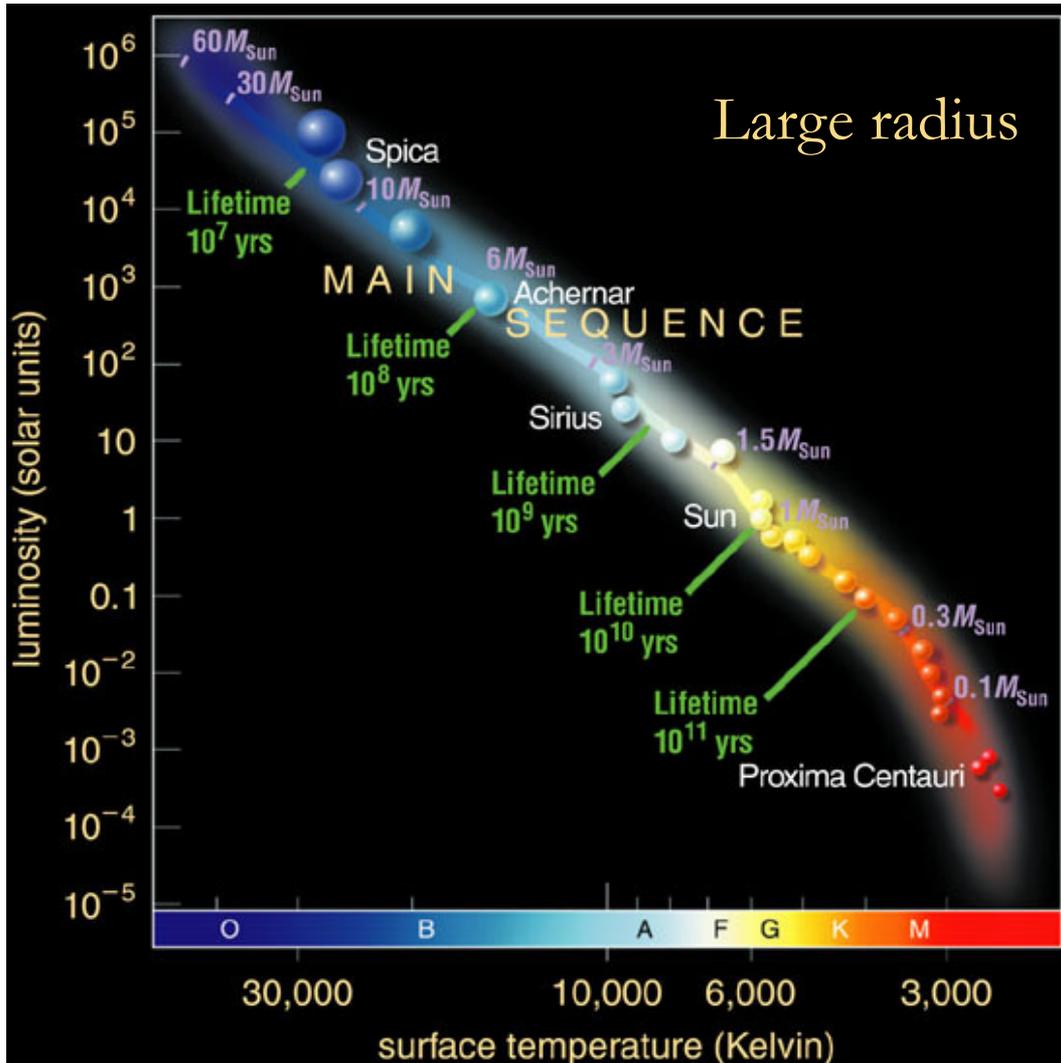


The Hertzsprung–Russell diagram



1. Most stars fall somewhere on the *main sequence* of the H-R diagram.

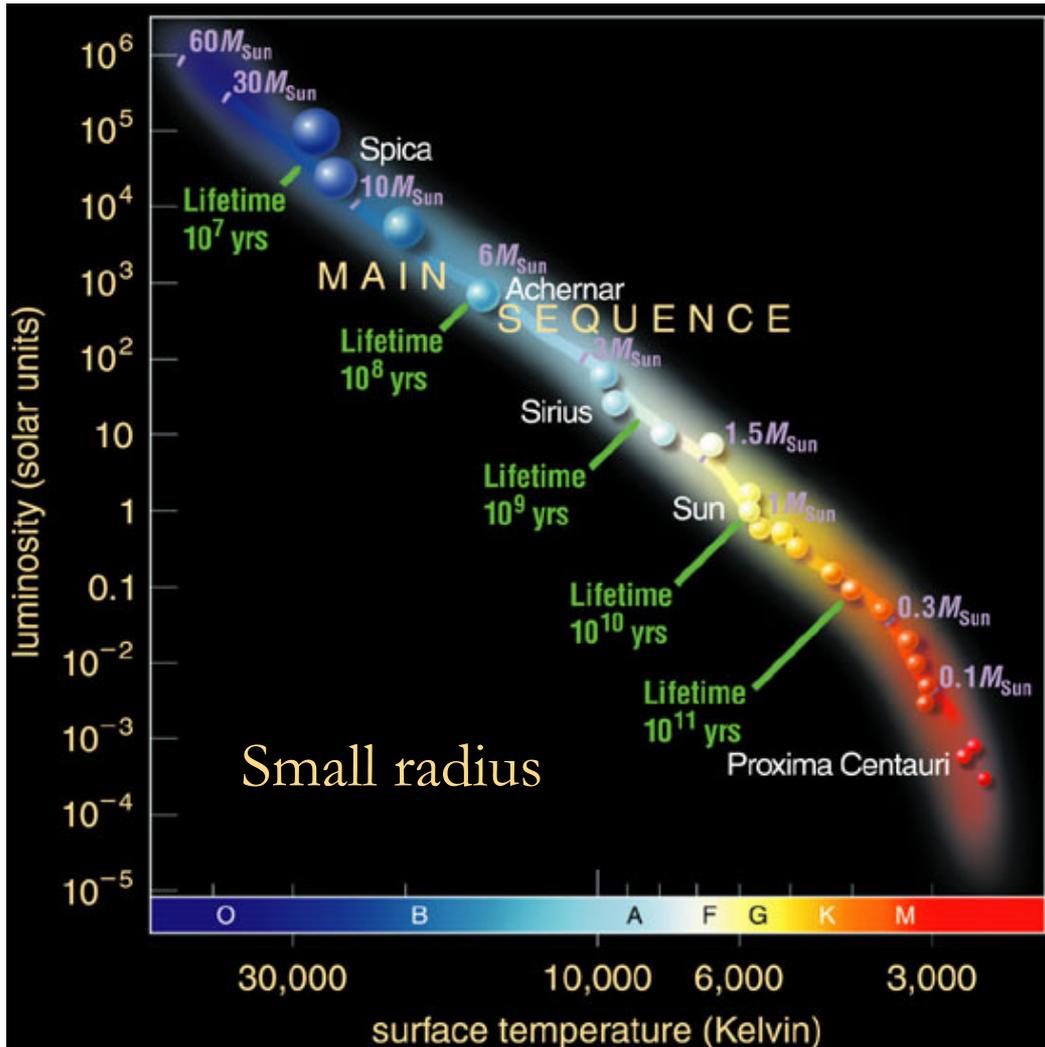
The Hertzsprung–Russell diagram



2. *Giants* and *Supergiants*

Stars with lower *Temp* and higher *Luminosity* than main-sequence stars must have **larger** radii.

The Hertzsprung–Russell diagram



3. *White dwarfs*

Stars with higher *Temp* and lower *Luminosity* than main-sequence stars must have **smaller radii**.

Spectral classification

A star's full classification includes **spectral type**:

(Hottest) O B A F G K M (Coolest)

(each class is subdivided from 0-9; the *higher* number is *cooler*)

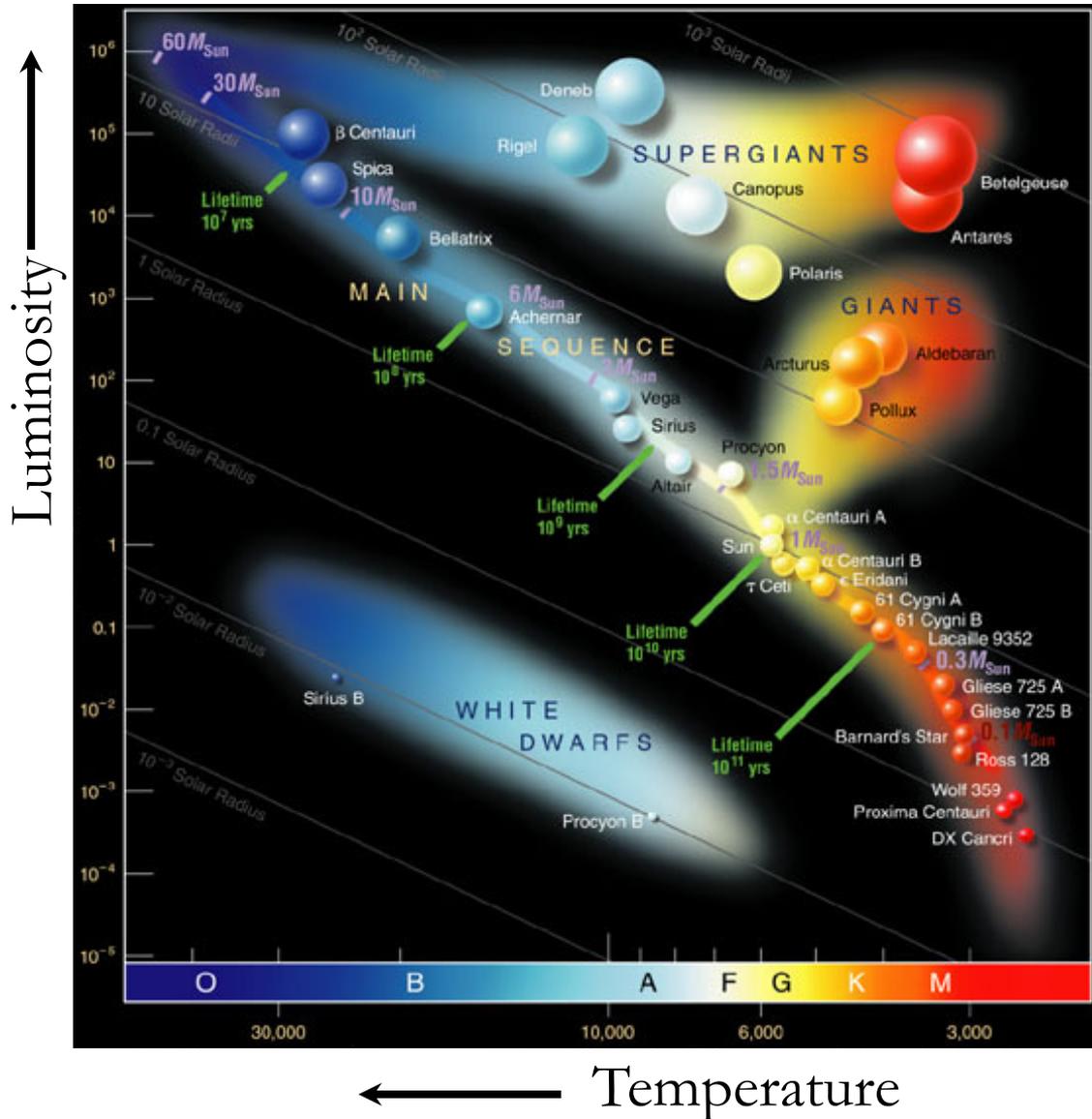
and **luminosity class** (related to the size of the star):

I	—	supergiant
II	—	bright giant
III	—	giant
IV	—	subgiant
V	—	main sequence
d	---	dwarf

Examples:

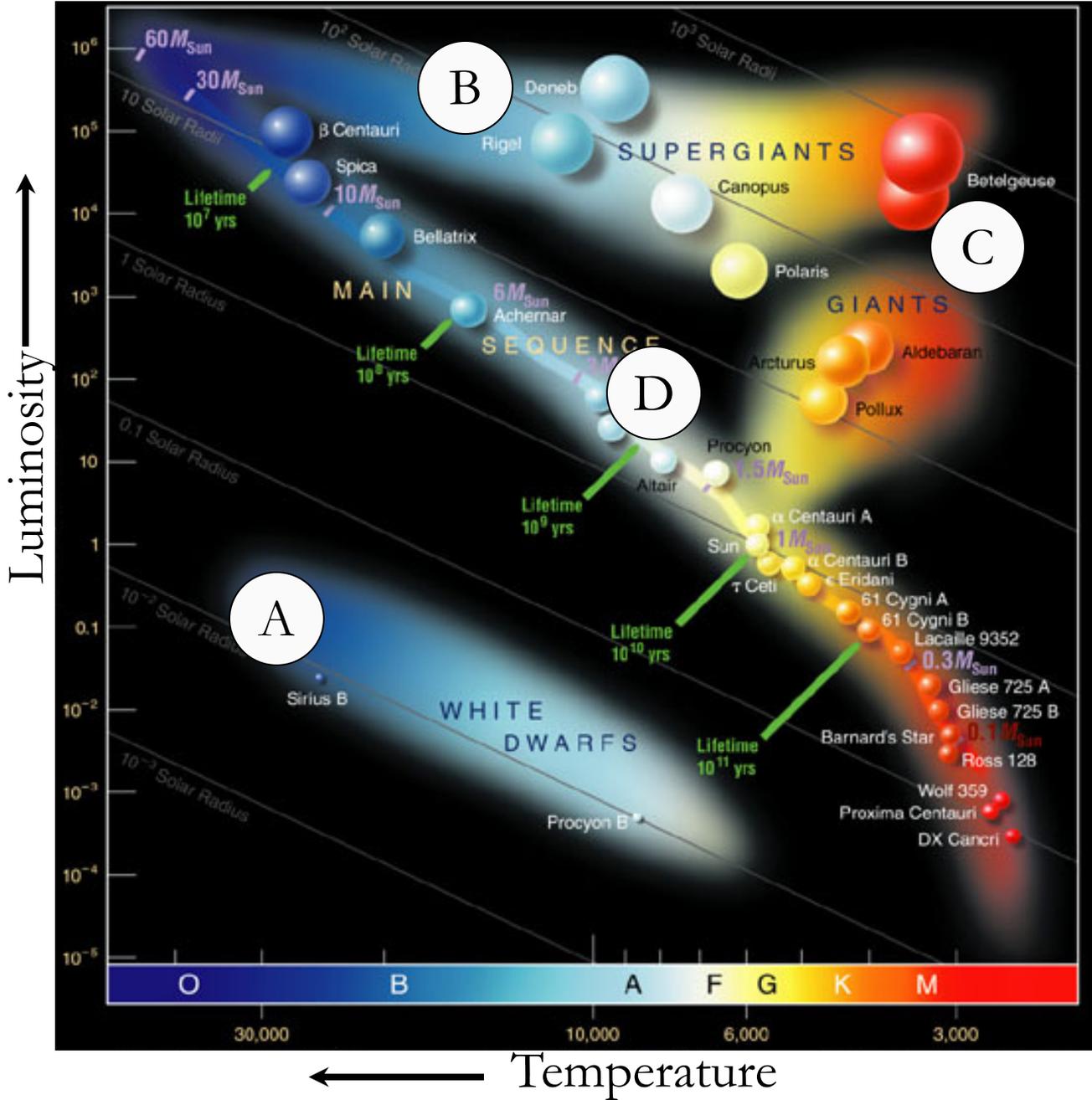
Sun	—	G2 V
Sirius	—	A1 V
Proxima Centauri	—	M5 V
Betelgeuse	—	M2 I

The Hertzsprung–Russell diagram

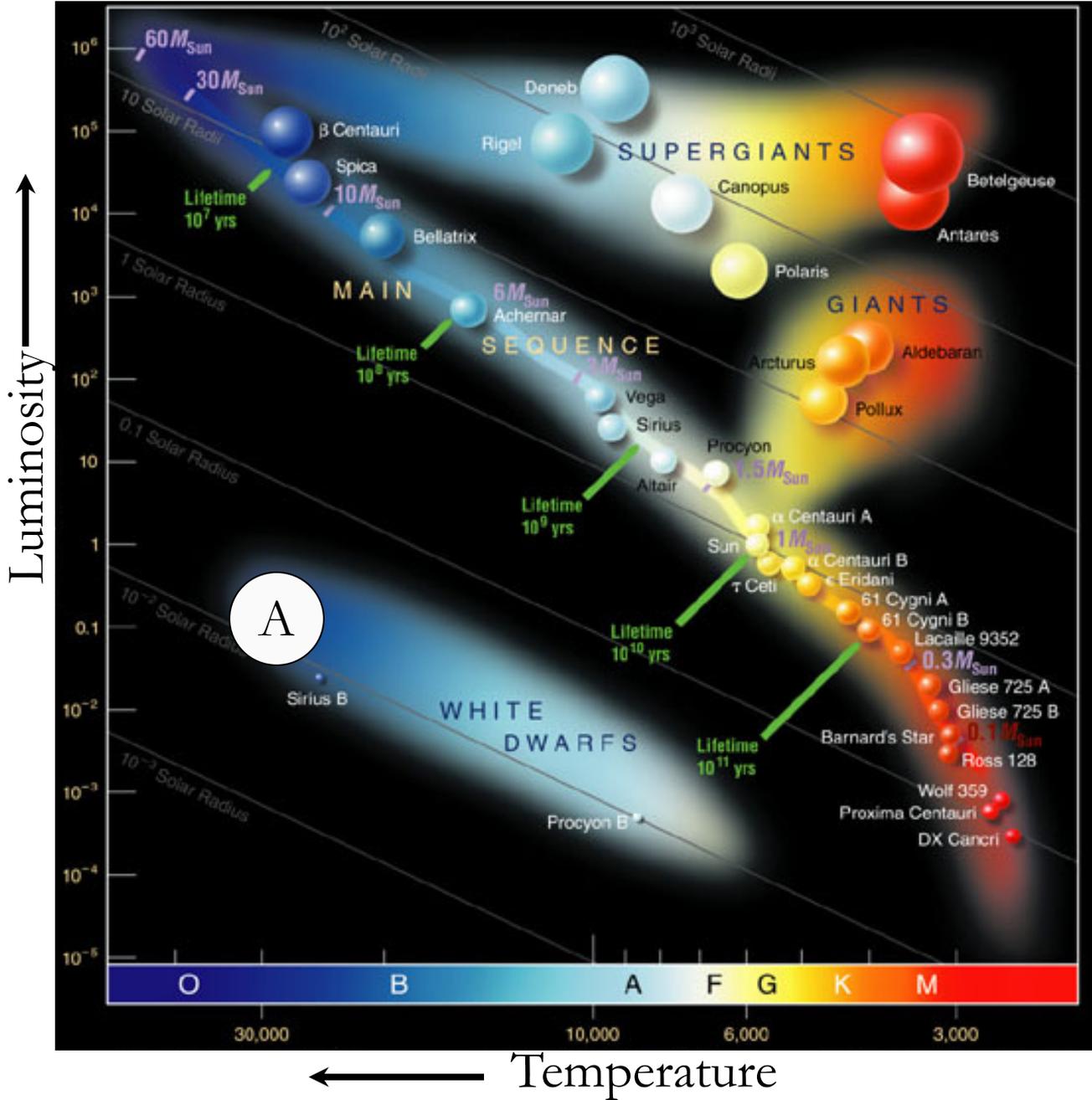


HR diagram depicts:

- Temperature
- Color
- Spectral type
- Luminosity
- Radius

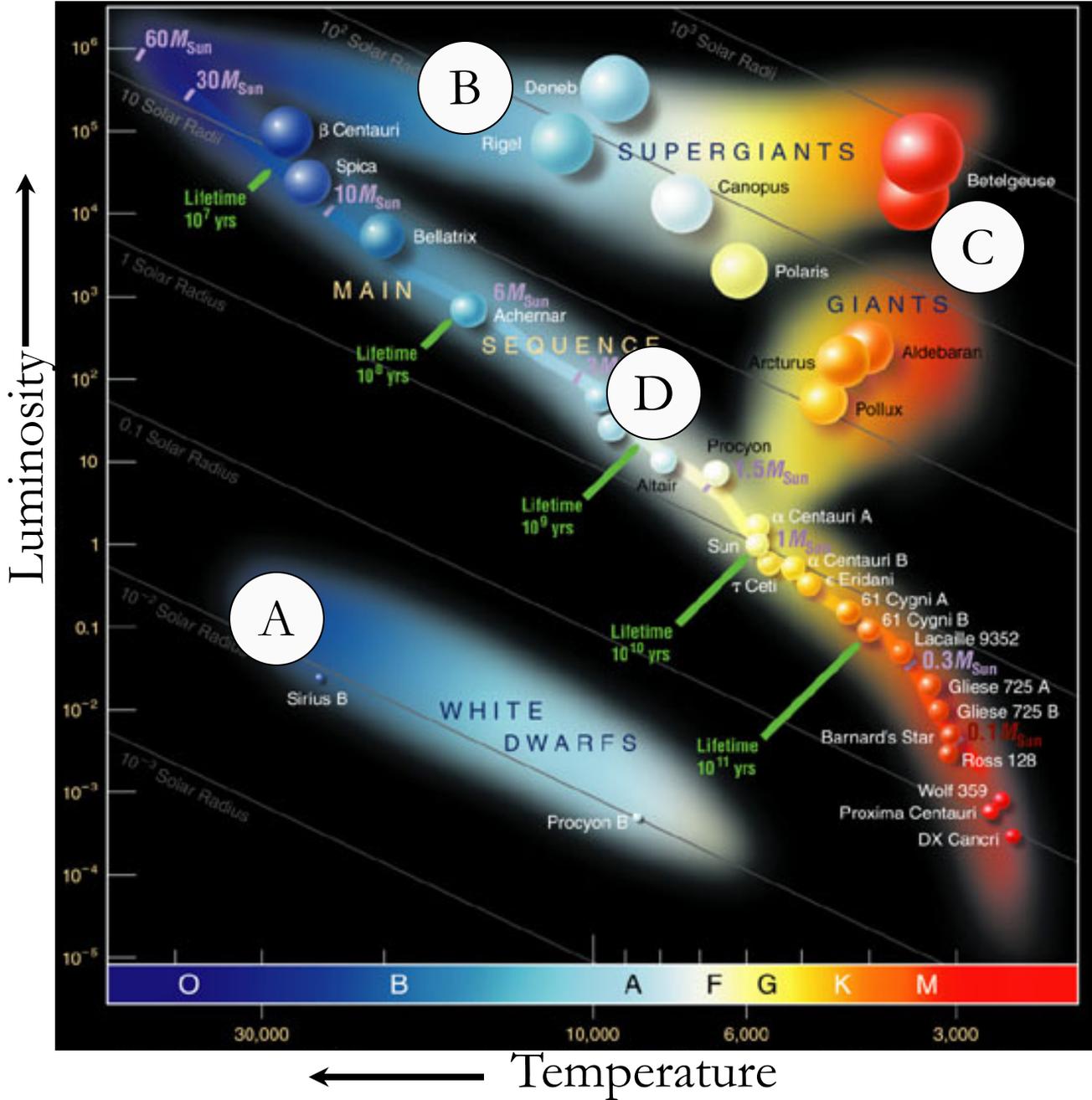


Which star is the hottest?

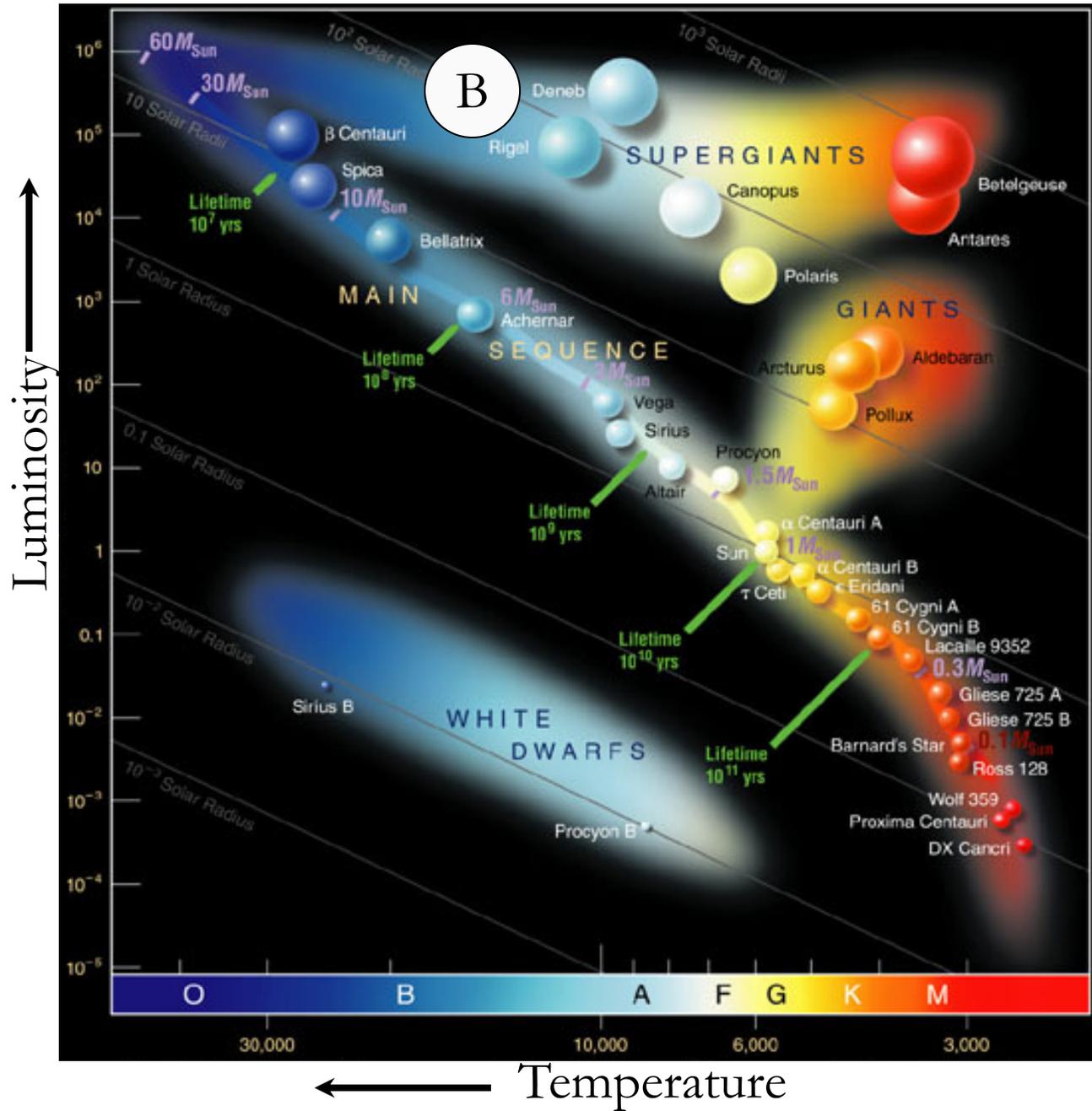


Which star is the hottest?

A

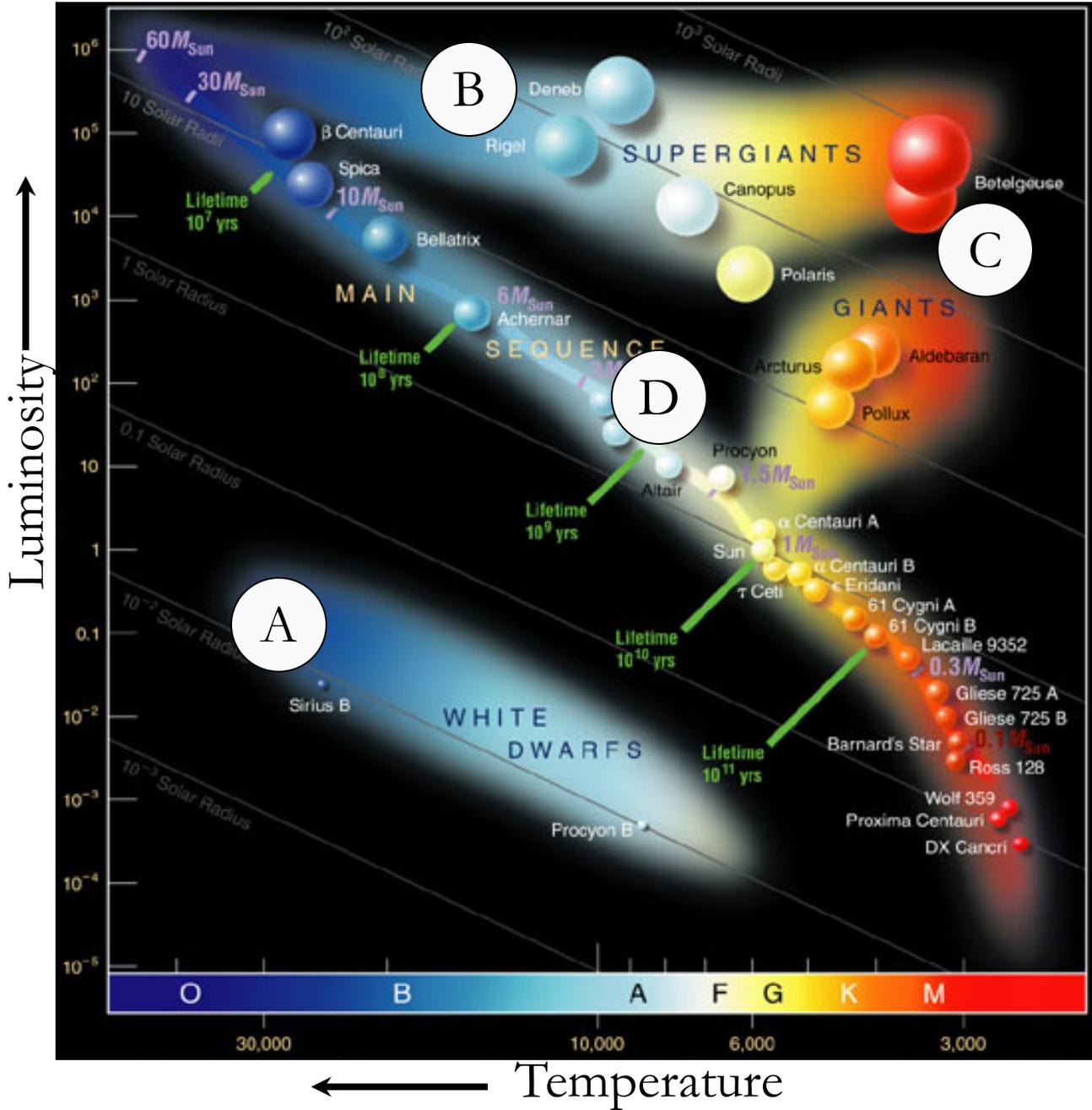


Which star is the most luminous?

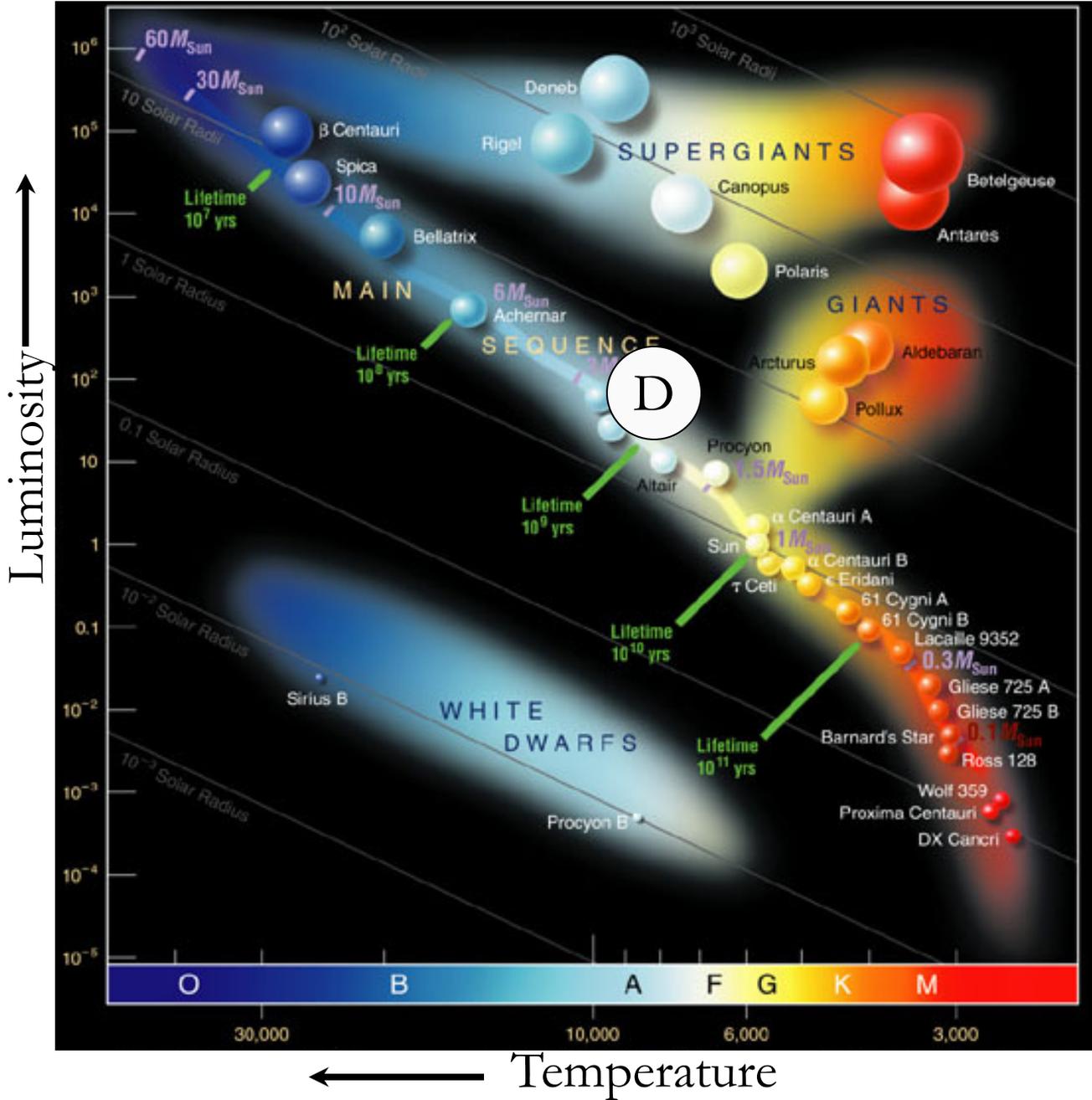


Which star is the most luminous?

B

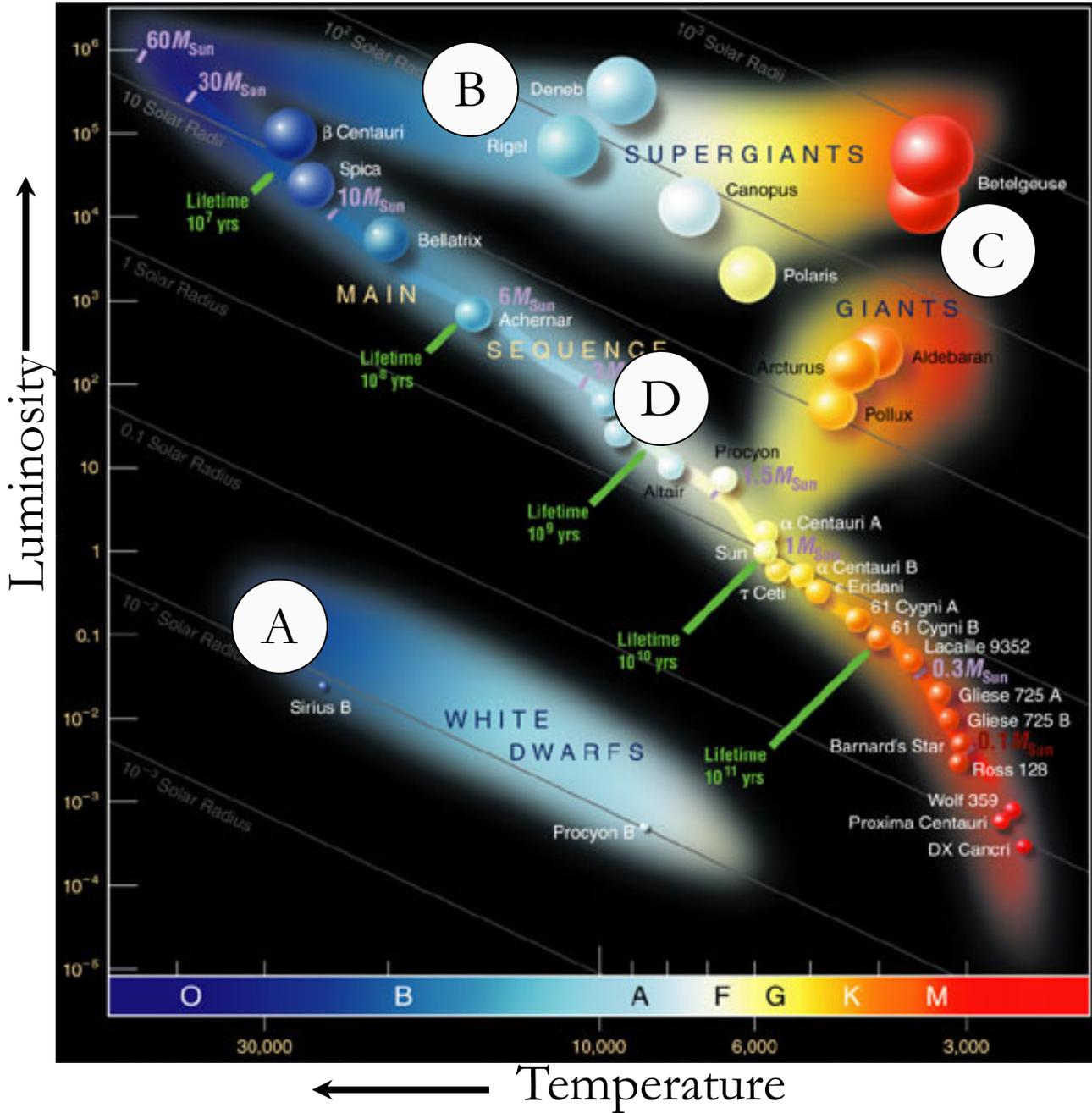


Which star is a main-sequence star?

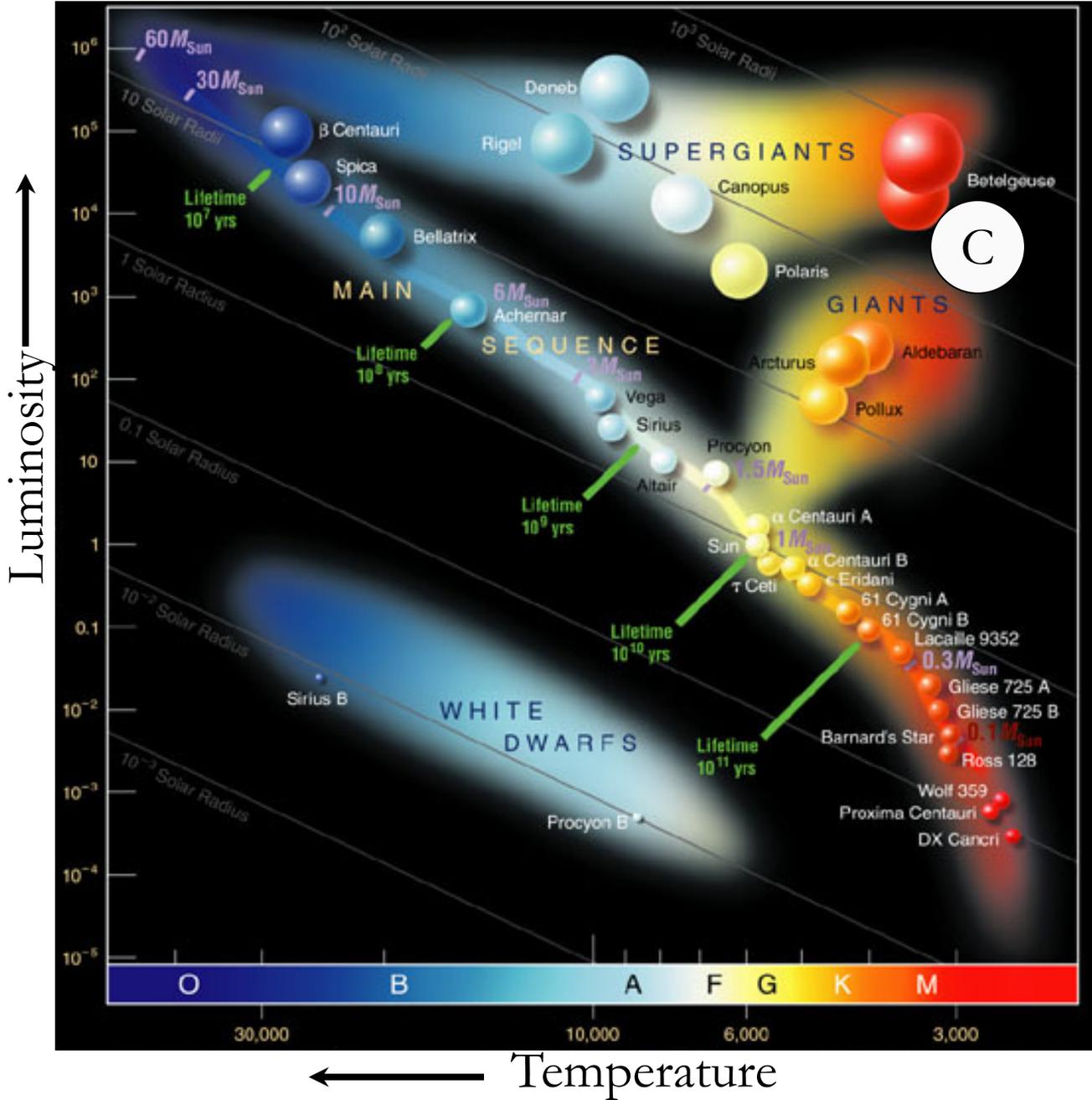


Which star is a main-sequence star?

D



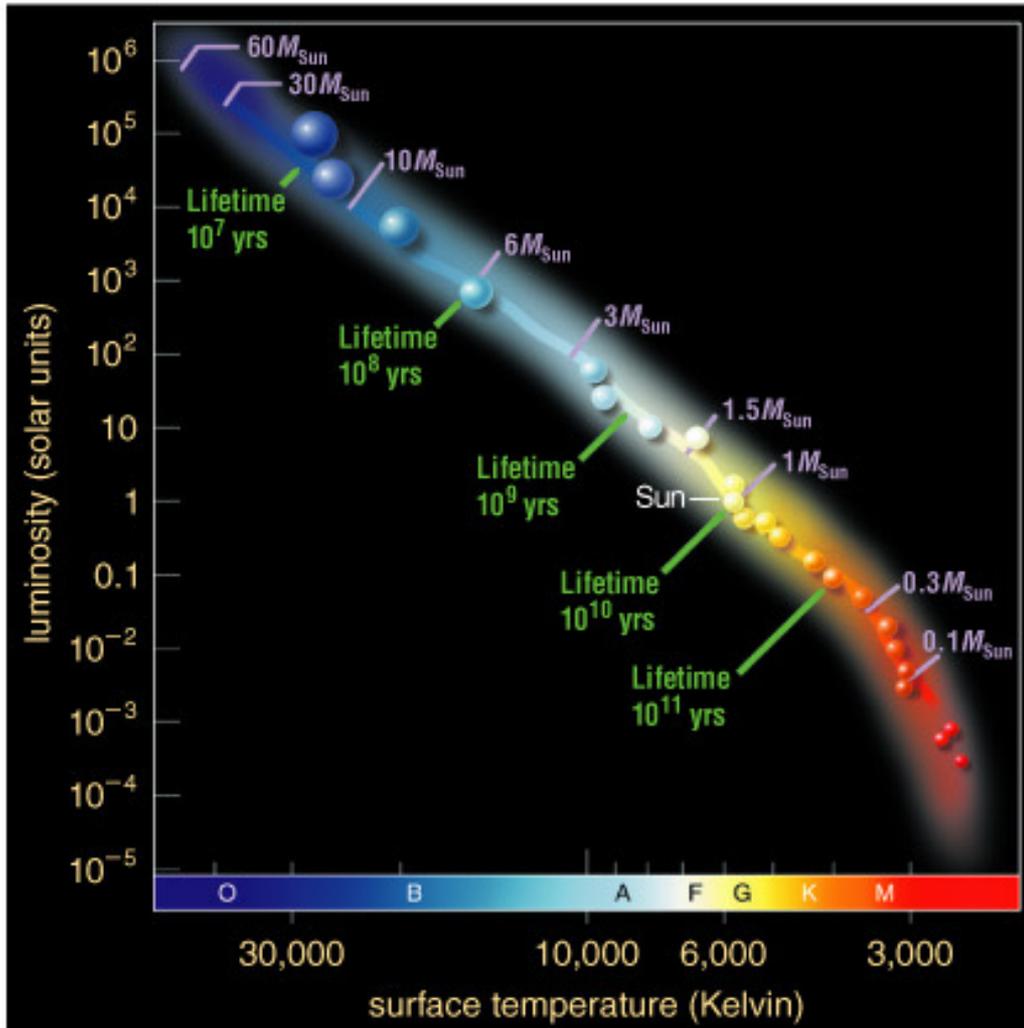
Which star has the largest radius?



Which star has the largest radius?

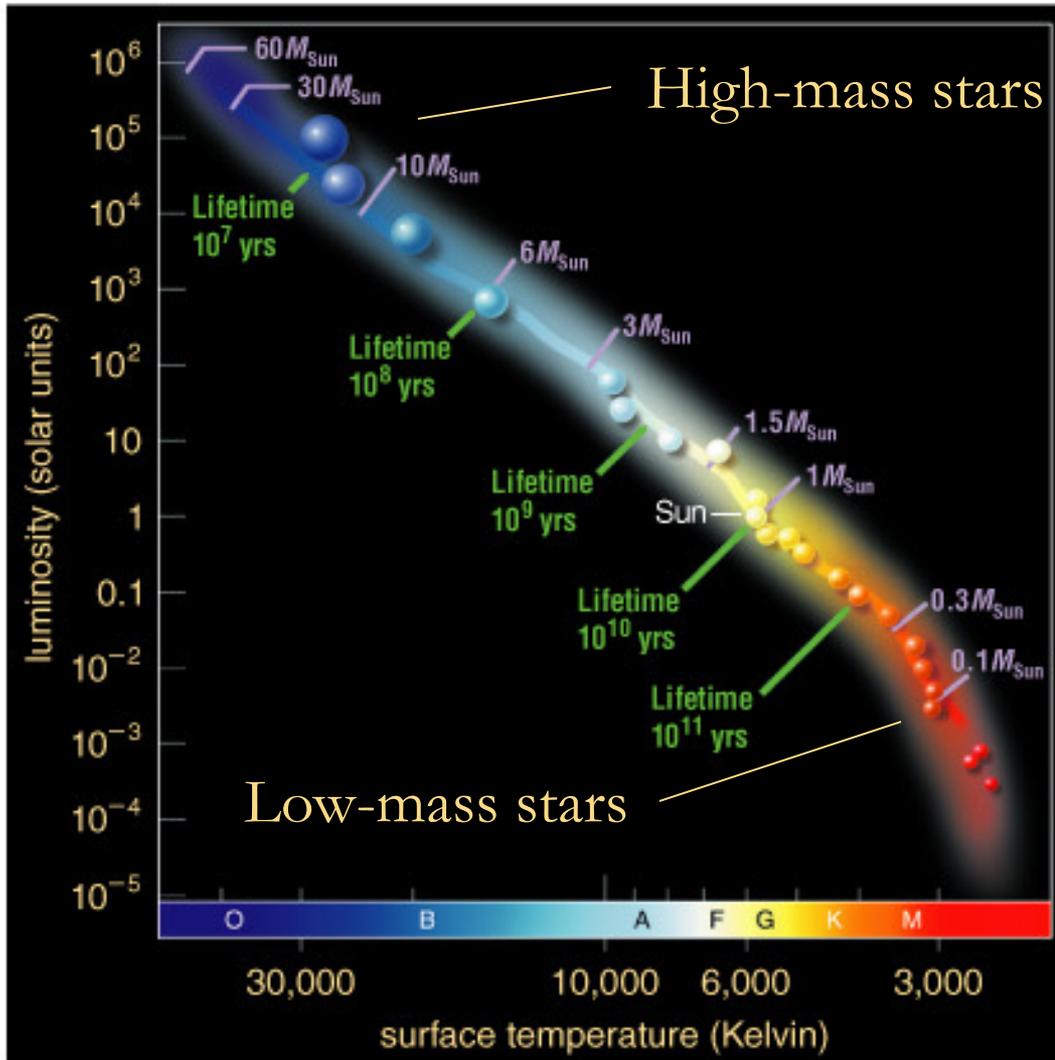
C

What is the significance of the main sequence?



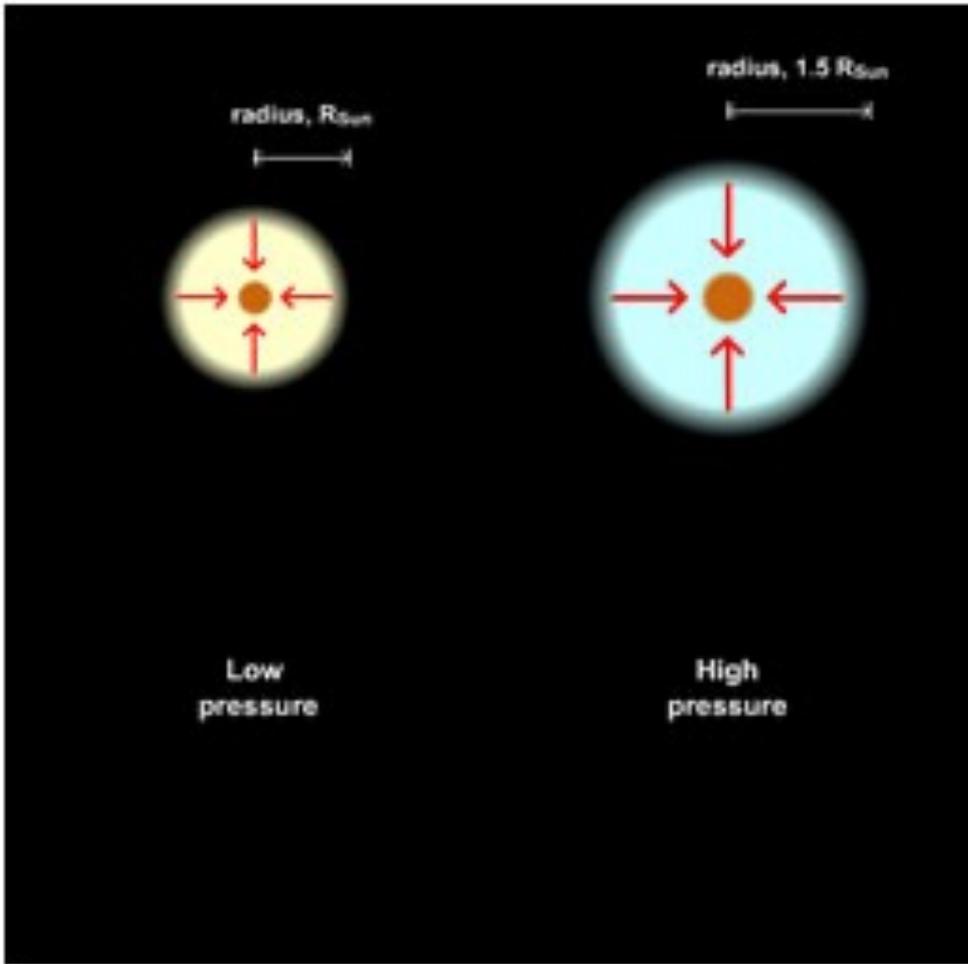
- *Main-sequence stars are fusing hydrogen into helium in their cores, like the Sun.*
- Luminous main-sequence stars are hot (blue).
- Less luminous ones are cooler (yellow or red).

What is the significance of the main sequence?



- Position along MS is related to *mass*
- Hot, blue stars are much more **massive** than the cool, red ones.
- Mass *decreases* as you go down and right on the main sequence.
- Range:
 $0.08 M_{\text{Sun}} - 150 M_{\text{Sun}}$

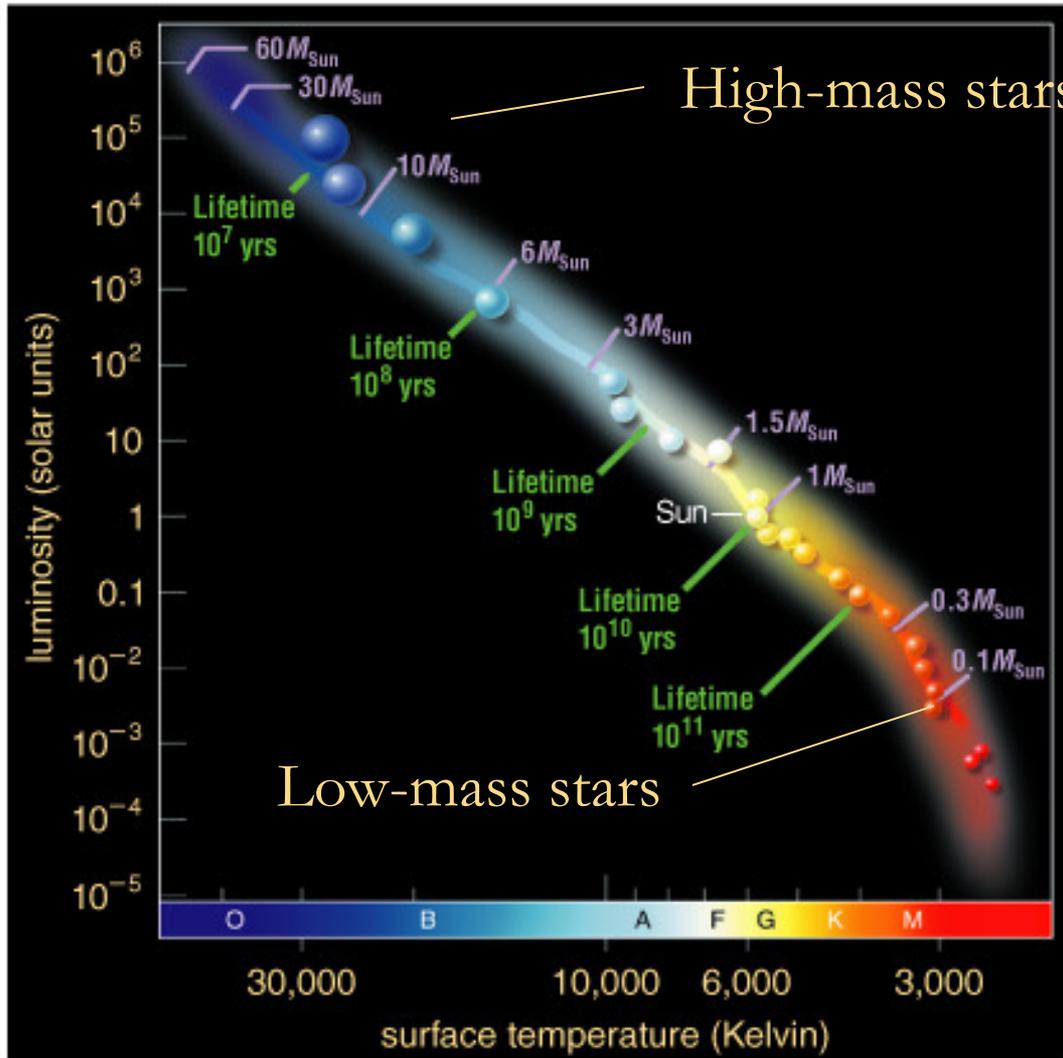
Pressure vs gravity



- The core pressure and temperature of a higher-mass star need to be higher in order to balance gravity.
- A higher core temperature boosts the fusion rate, leading to greater luminosity.

Hydrostatic Equilibrium

What is the significance of the main sequence?



- 1) The **mass** of a normal, hydrogen-burning star determines its fusion rate.
- 2) Fusion rate determines the star's luminosity and spectral type (temperature).
- 3) Fusion rate and thus luminosity are very sensitive to mass.
- 4) Fusion rate has great effect on lifetime!

Mass is most important stellar property

Stellar Properties Review

Luminosity: found from brightness and distance

($0.08 M_{\text{Sun}}$) $10^{-4} L_{\text{Sun}} - 10^6 L_{\text{Sun}}$ ($150 M_{\text{Sun}}$)

Temperature: found from color and spectral type

($0.08 M_{\text{Sun}}$) 3,000 K – 50,000 K ($150 M_{\text{Sun}}$)

Mass: found from period (p) and average separation (a)
of binary-star orbit

$0.08 M_{\text{Sun}} - 150 M_{\text{Sun}}$

Mass and Lifetime

Sun's life expectancy: 10 billion years

Life expectancy of a $10 M_{Sun}$ star:

10 times as much fuel, uses it 10^4 times as fast

10 billion years $\times 10/10^4 \sim$ 10 million years

Life expectancy of a $0.1 M_{Sun}$ star:

0.1 times as much fuel, uses it 0.01 times as fast

10 billion years $\times 0.1/0.01 \sim$ 100 billion years

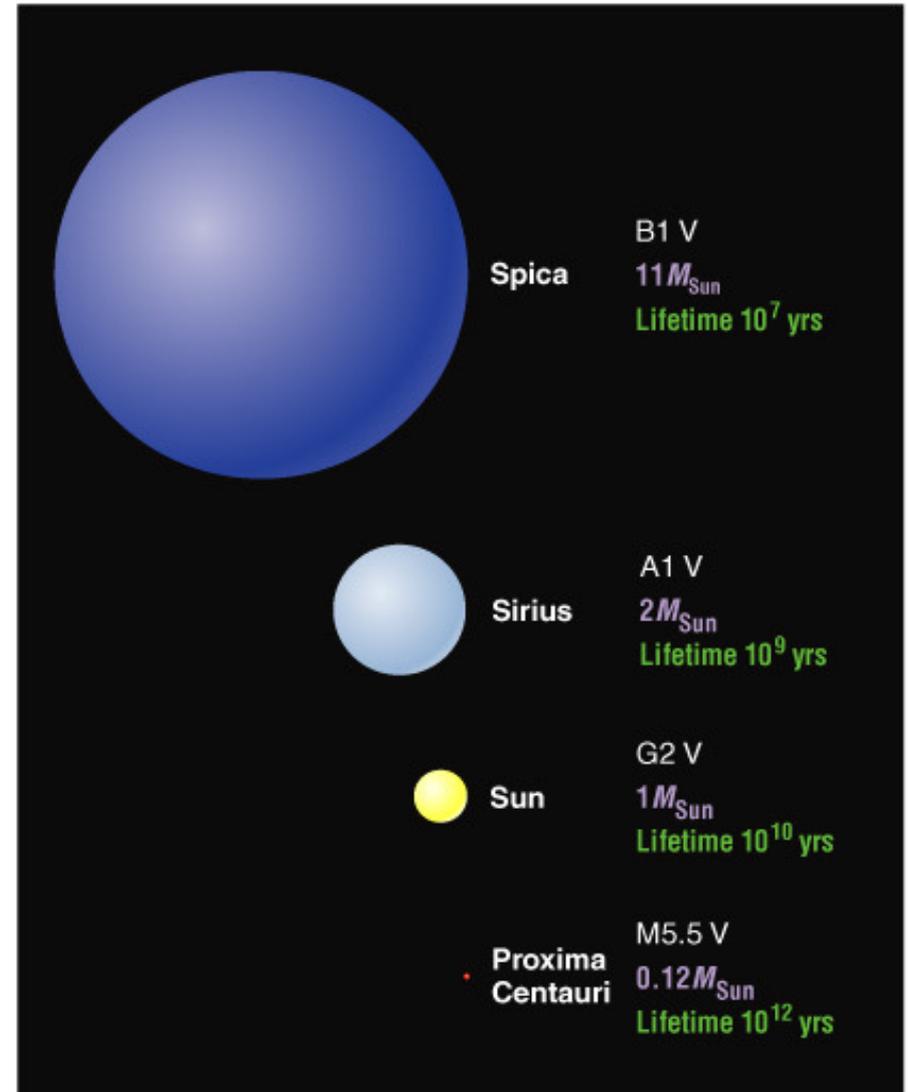
Main-Sequence Star Summary

High-mass:

- High luminosity
- Short-lived
- Large radius
- Blue

Low-mass:

- Low luminosity
- Long-lived
- Small radius
- Red

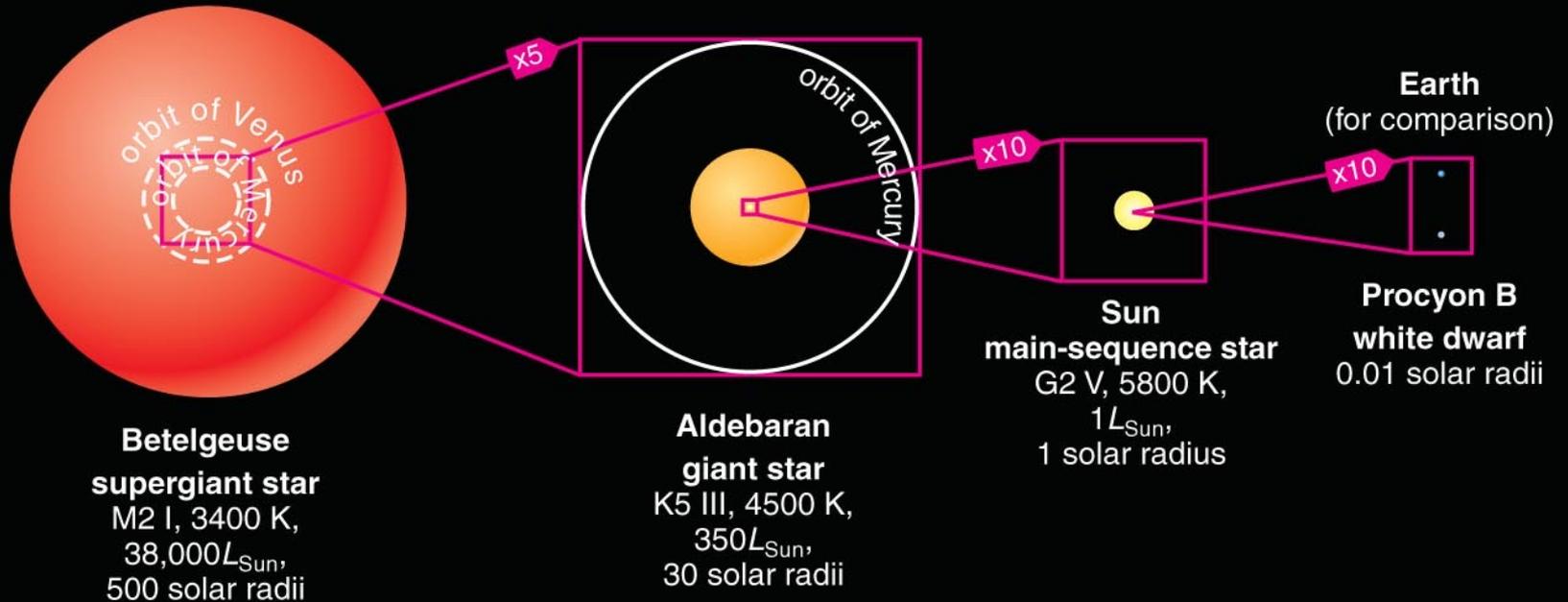


What are giants, supergiants, and white dwarfs?

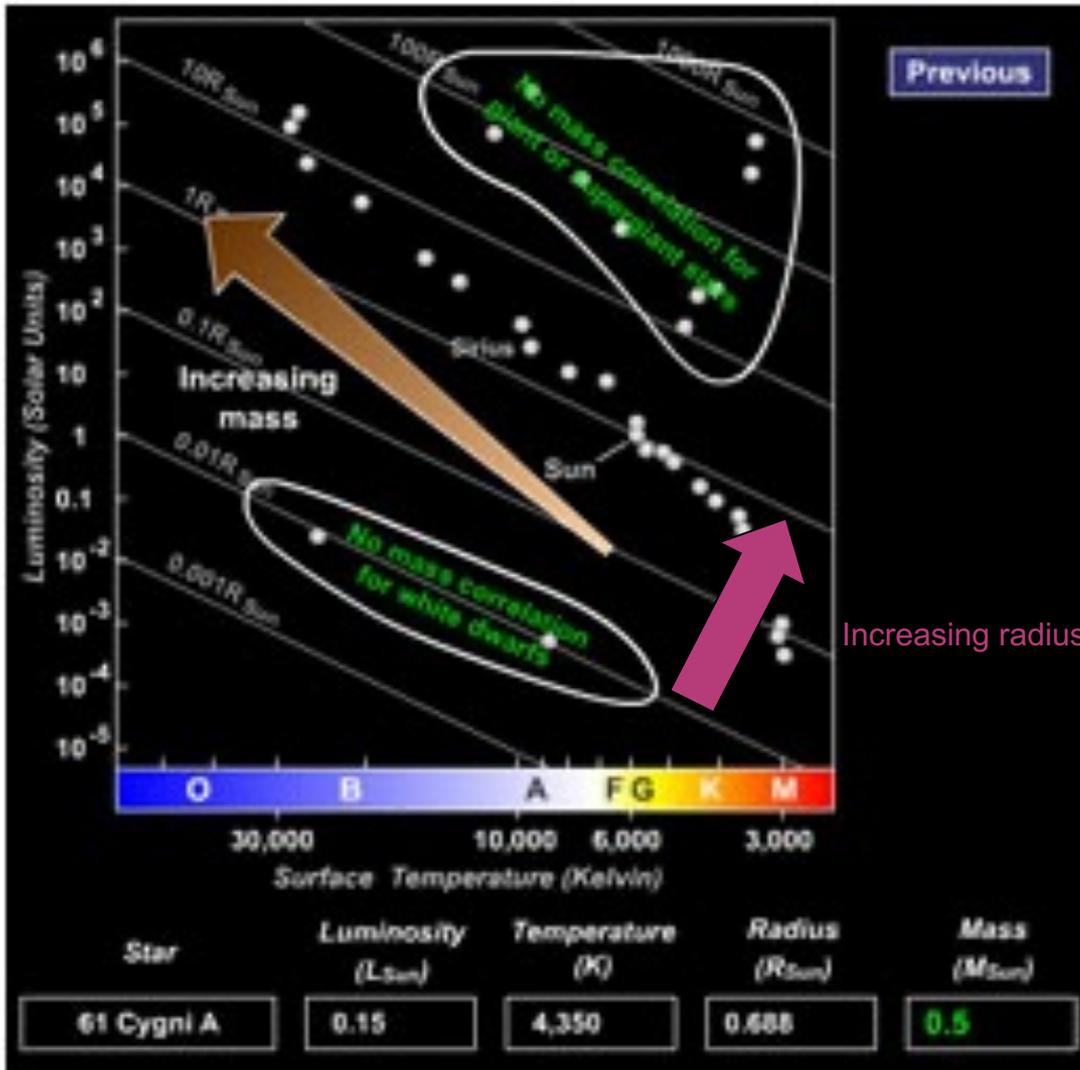


Sizes of Giants and Supergiants

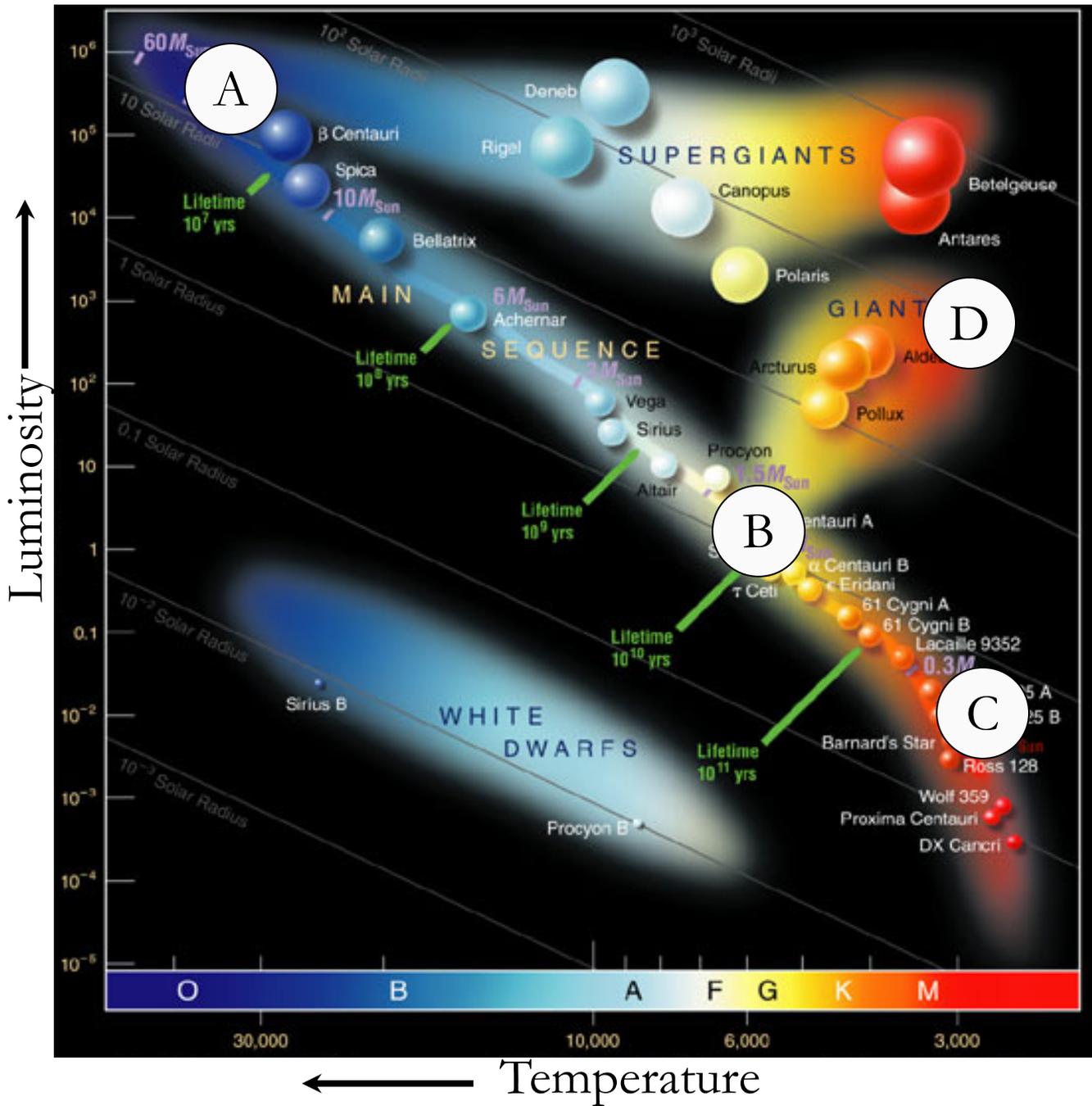
Relative Sizes of Stars from Supergiants to White Dwarfs



Relationship between Main-Sequence Stellar Masses, Radii, and Location on H-R Diagram



- **Mass** increases to the upper left *on the Main Sequence*
- **Radius** increases to the upper right



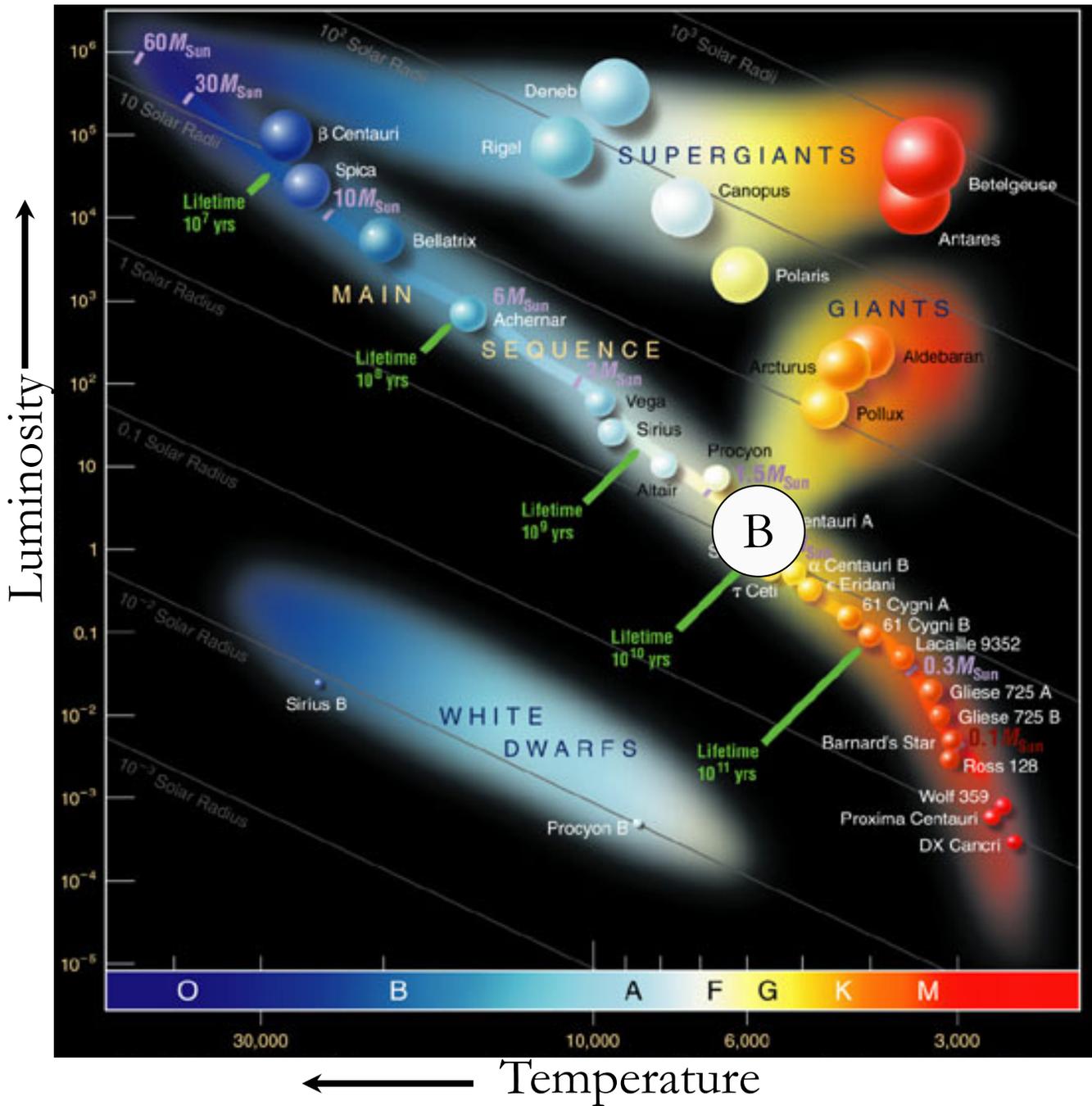
Which star is most like our Sun?

A

D

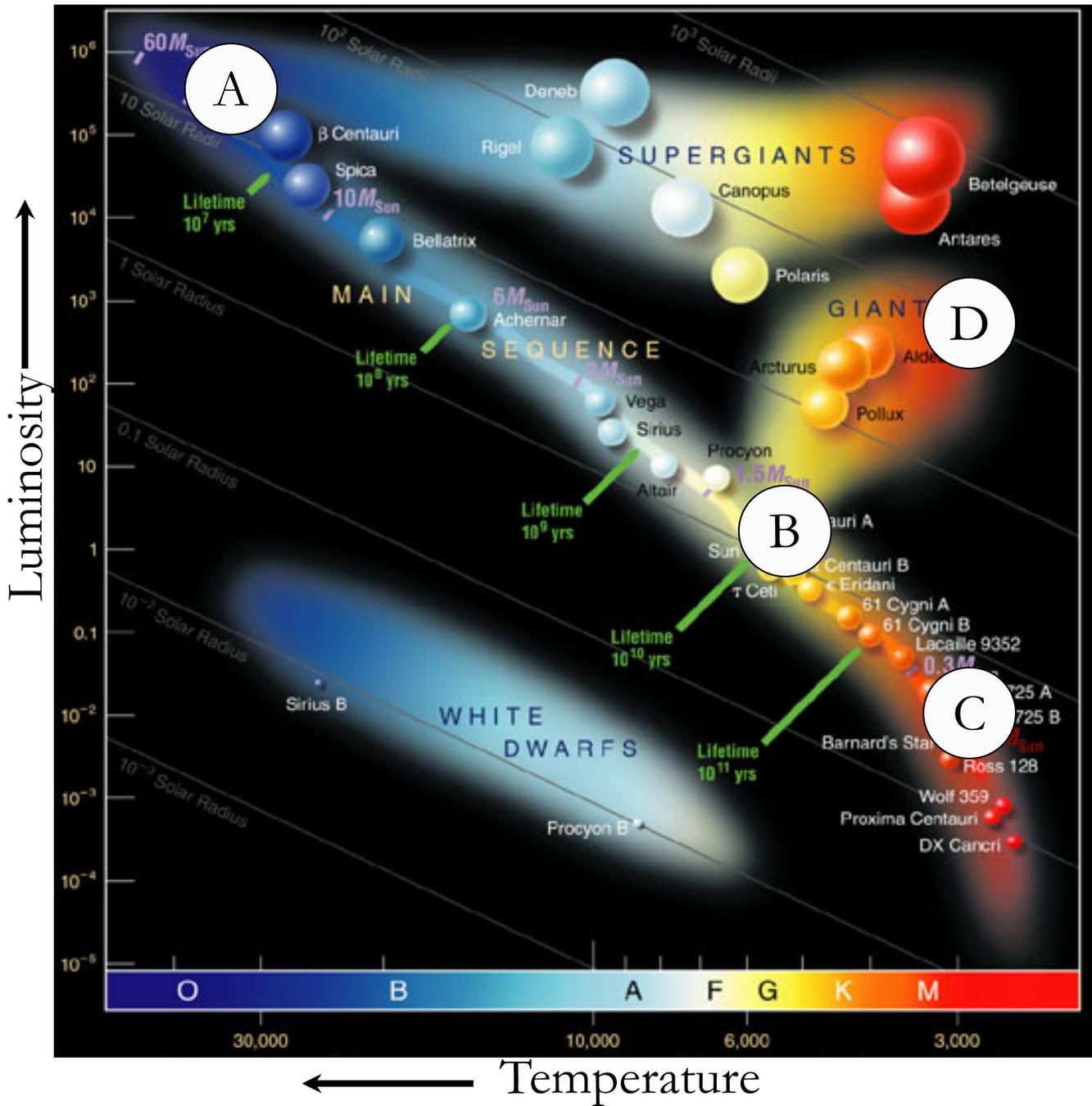
B

C



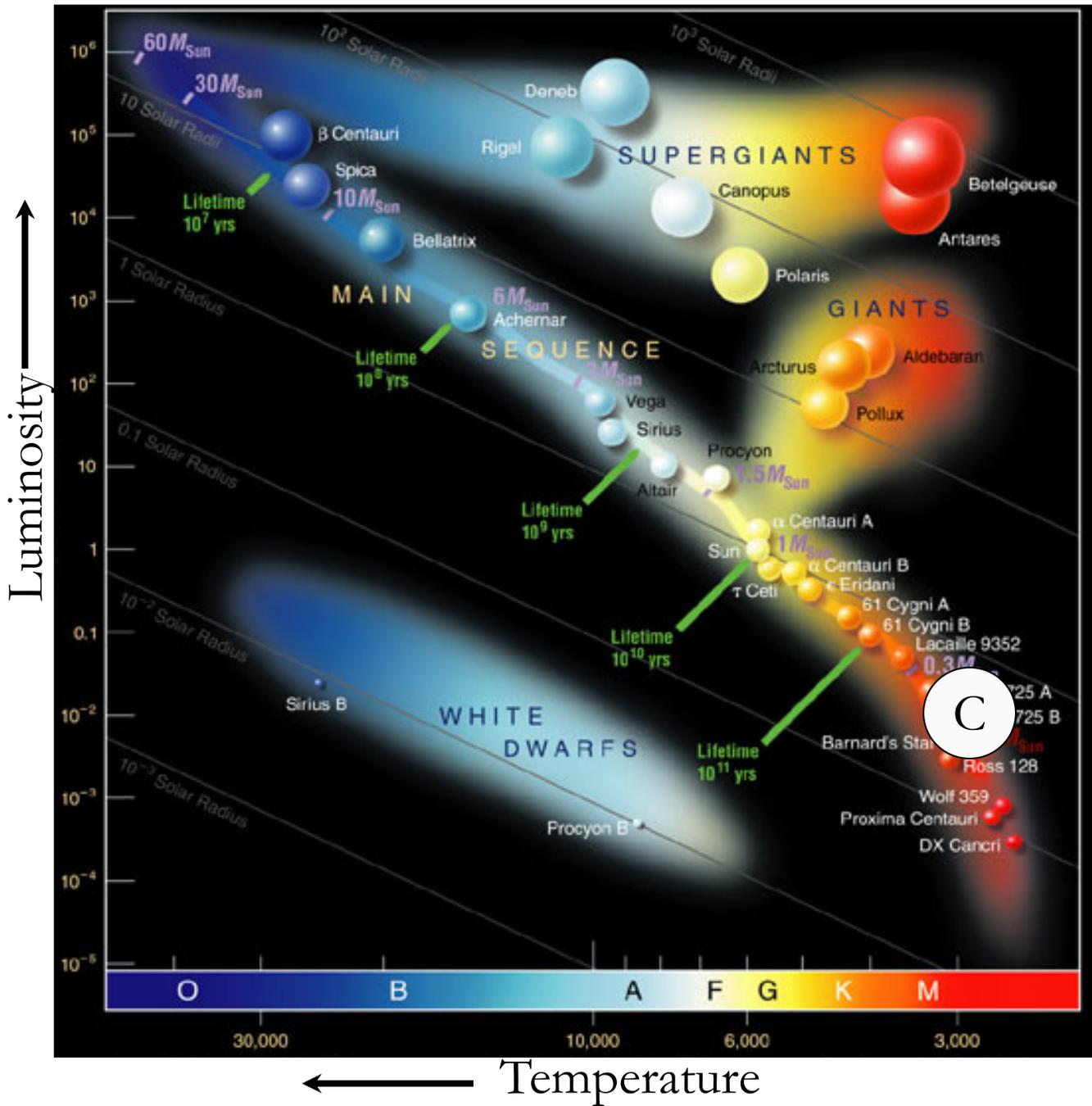
Which star is most like our Sun?

B



Which of these stars will have changed the least 10 billion years from now?

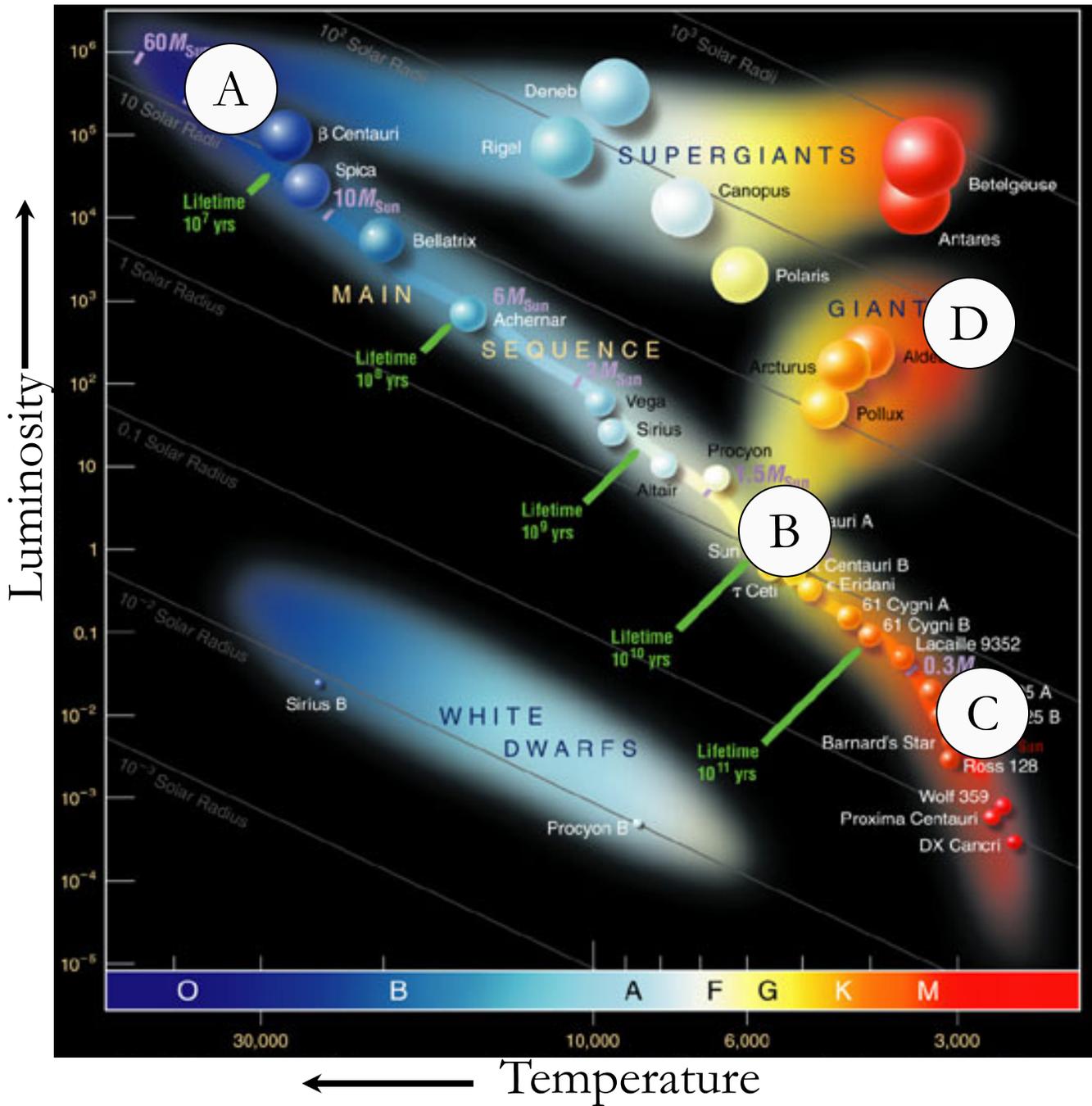
← Temperature



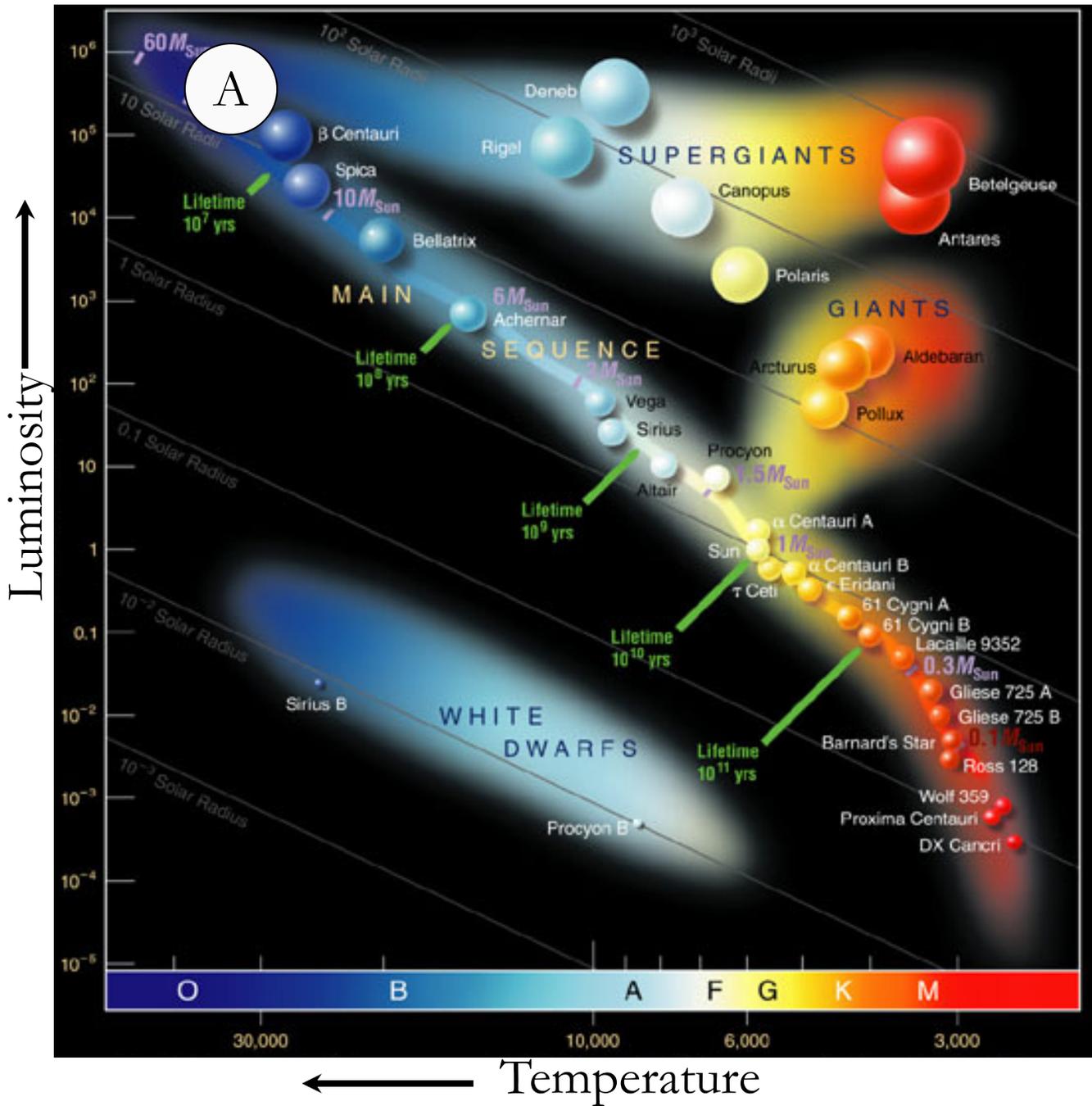
Which of these stars will have changed the least 10 billion years from now?

C

C



Which of these stars can be no more than 10 million years old?



Which of these stars can be no more than 10 million years old?

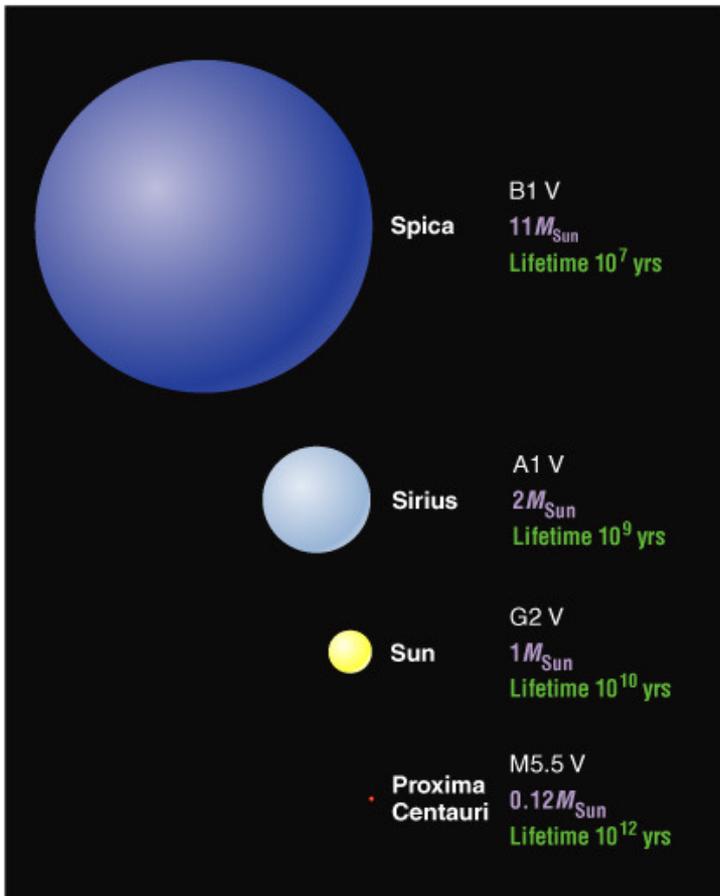
A

Off the Main Sequence

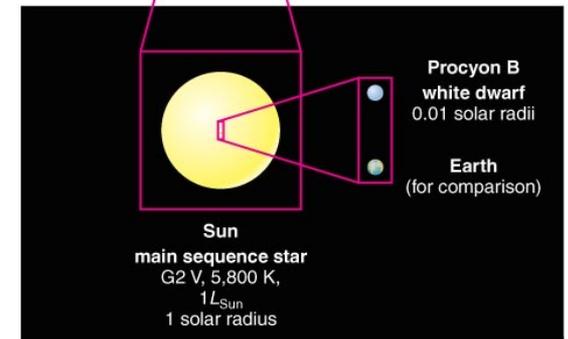
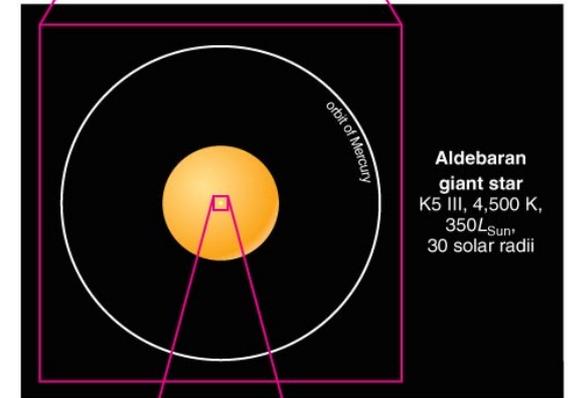
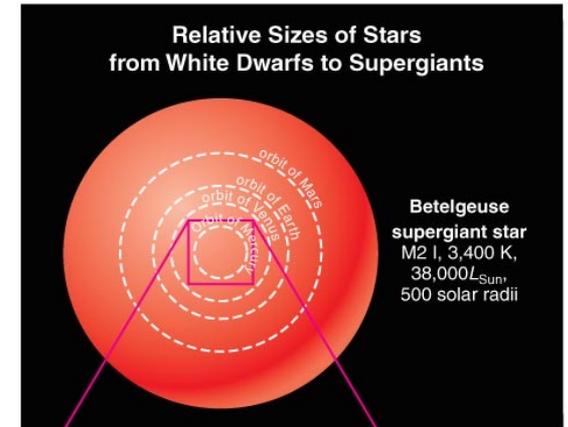
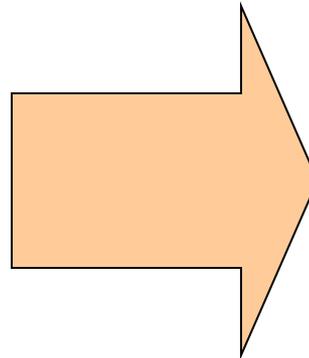
- Stellar properties depend on both **mass** and **age**: *those that have finished fusing H to He in their cores are no longer on the main sequence.*
- *All* stars become larger and redder after exhausting their core hydrogen and become **giants** and **supergiants**. These are cooler but more luminous than MS stars, larger in radius.
- Low mass stars end up small after fusion has ceased. They eject their outer layers and become **white dwarfs**.

Off the Main Sequence

As stars use up their hydrogen fuel, *they leave the main sequence* to become giants, supergiants, and white dwarfs



Main-sequence stars (to scale)



Giants, supergiants, white dwarfs

What have we learned?

Begin 3 minute review

What have we learned?

What is a Hertzsprung–Russell diagram?

An H-R diagram plots the stellar **luminosity** of stars versus surface **temperature** (or color or spectral type).

What is the significance of the main sequence?

Normal stars that fuse H to He in their cores fall on the **main sequence** of an H-R diagram.

A star's **mass** determines its position along the main sequence (high mass: luminous and blue; low mass: faint and red).

What have we learned?

What are giants, supergiants, and white dwarfs?

All stars become larger and redder after core hydrogen burning is exhausted: **giants** and **supergiants**.

Most stars end up as tiny **white dwarfs** after fusion has ceased.

What are the two types of star clusters?



- Stars usually form in groups or clusters.
- They are extremely useful to study because (1) they are at the same **distance** and (2) they are the same **age**, (3) they have the same **composition**.
- This allows us to compare them easily and accurately.

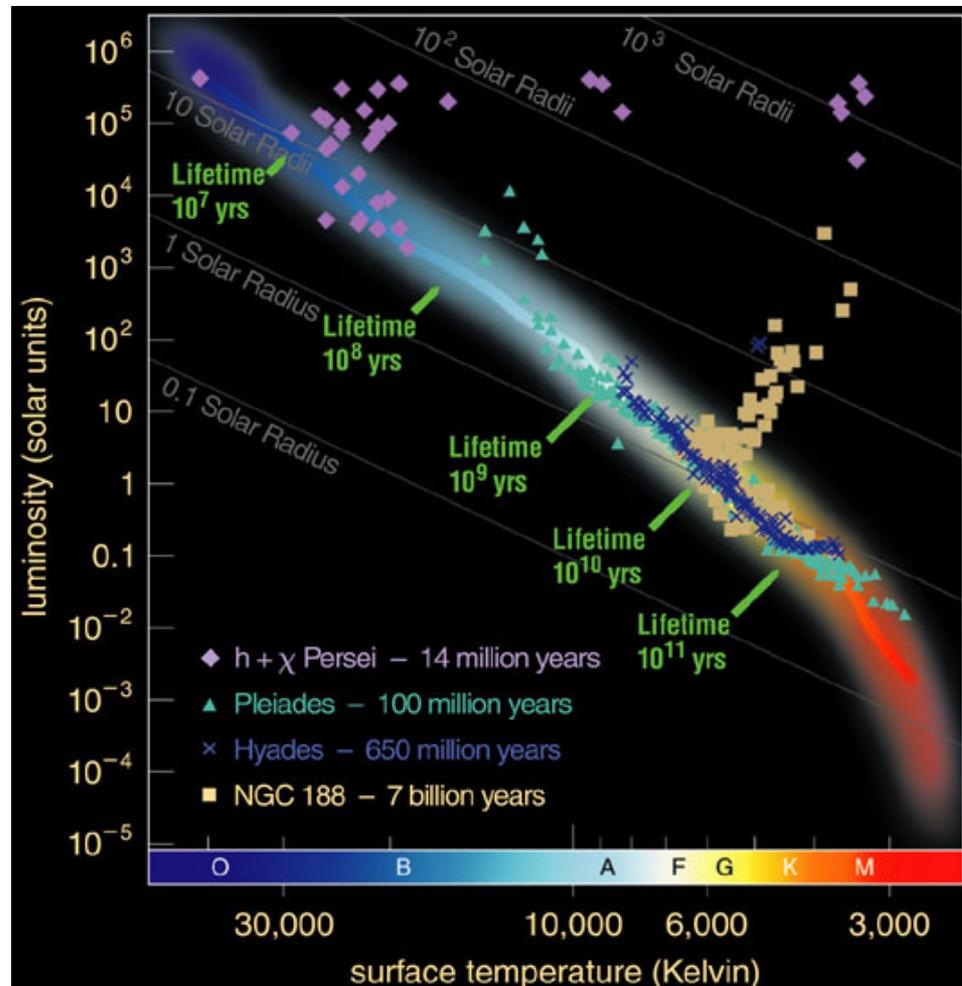
Open clusters

- A few thousand loosely packed stars
- Found within spiral arms of galaxy
- Young stars

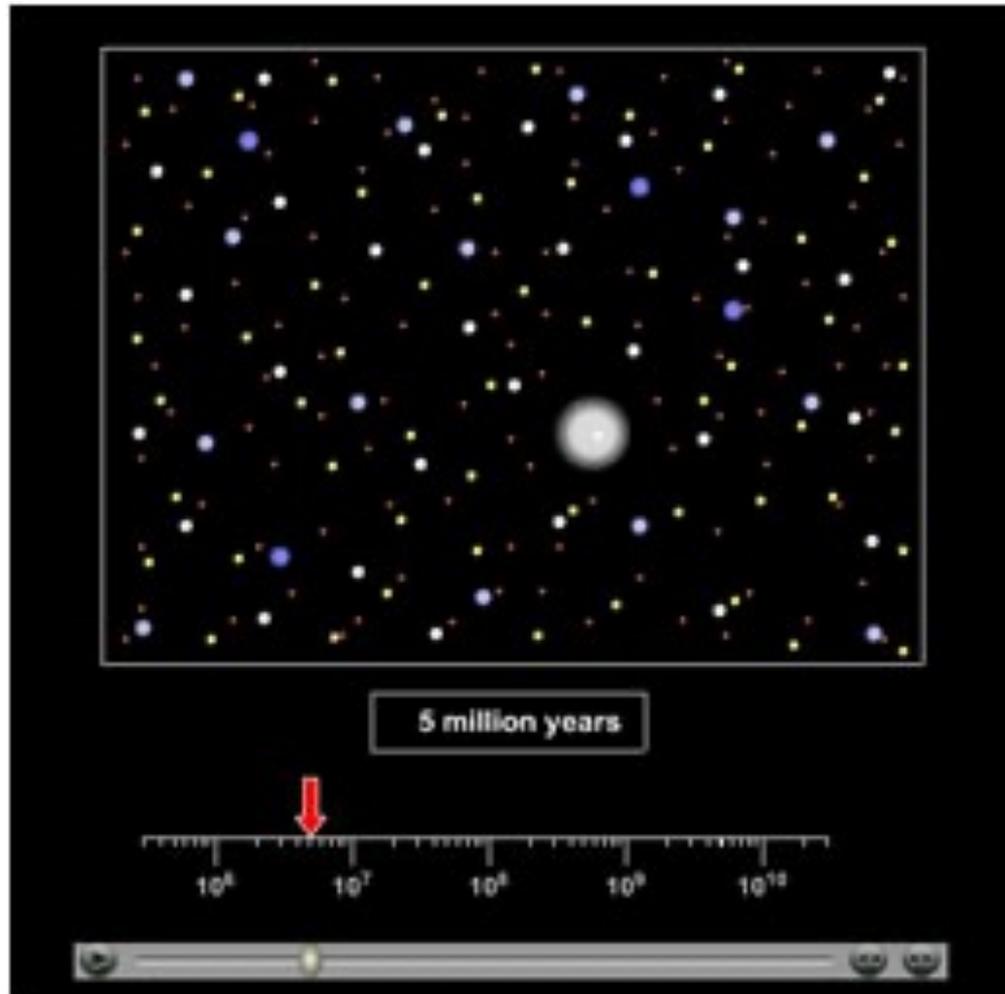
Globular clusters

- Hundreds of thousands of stars in a dense ball bound together by gravity
- Found orbiting outside a galaxy
- Old stars

How do we measure the age of a star cluster?



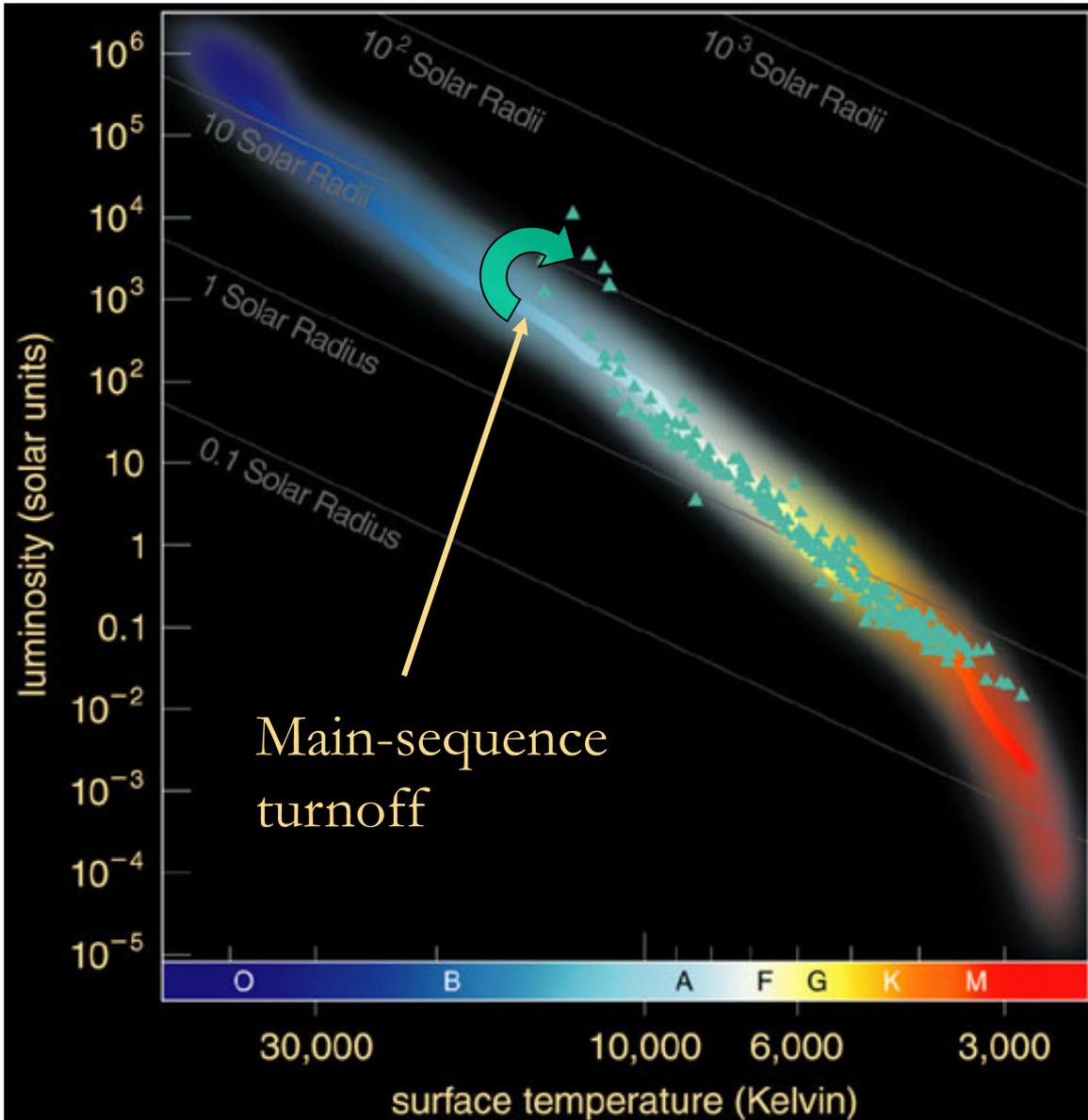
Stellar evolution



- Stars evolve by mass:
- Massive blue stars die first, followed by white, yellow, orange, and then red stars.
- Current remaining stars give us age of cluster!

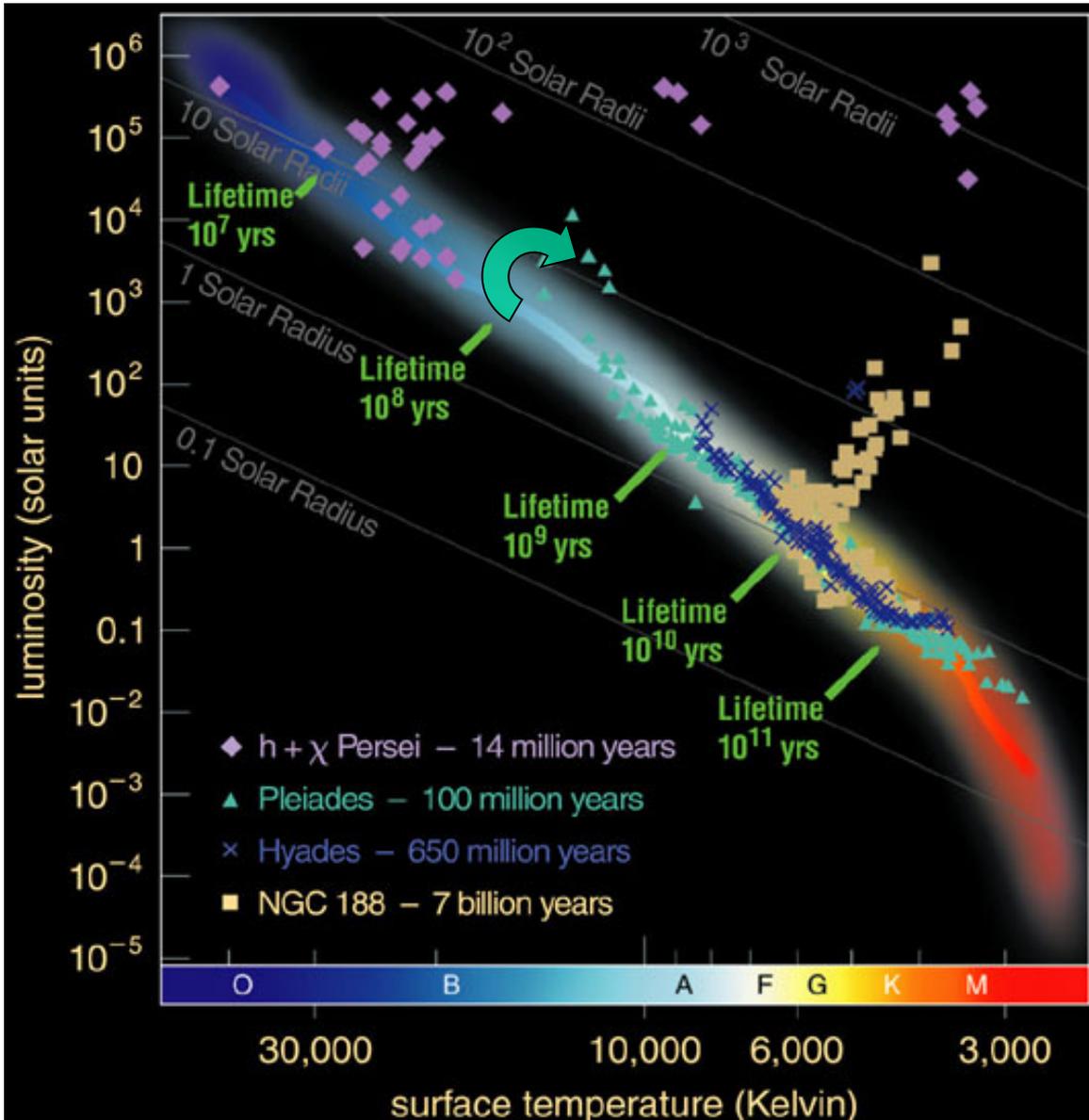
Visual Representation of a Star Cluster Evolving

The turn-off point



- We can plot a HR diagram *just for a cluster* and note the main sequence.
- As cluster stars use up hydrogen, they evolve off the main sequence towards the upper right and become giants or supergiants

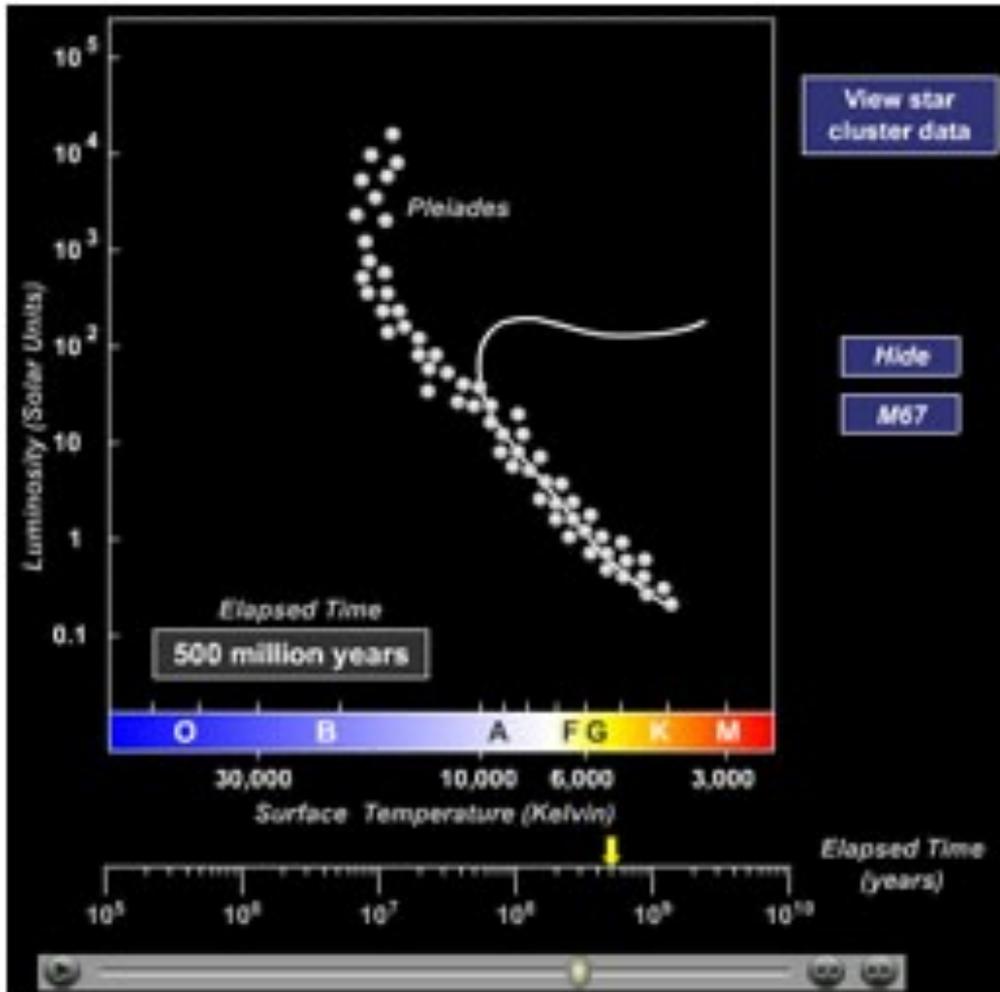
The turn-off point



*The main-sequence
turnoff point of a
cluster tells us its age.*

Pleiades cluster now has no stars with life expectancy less than around 100 million years.

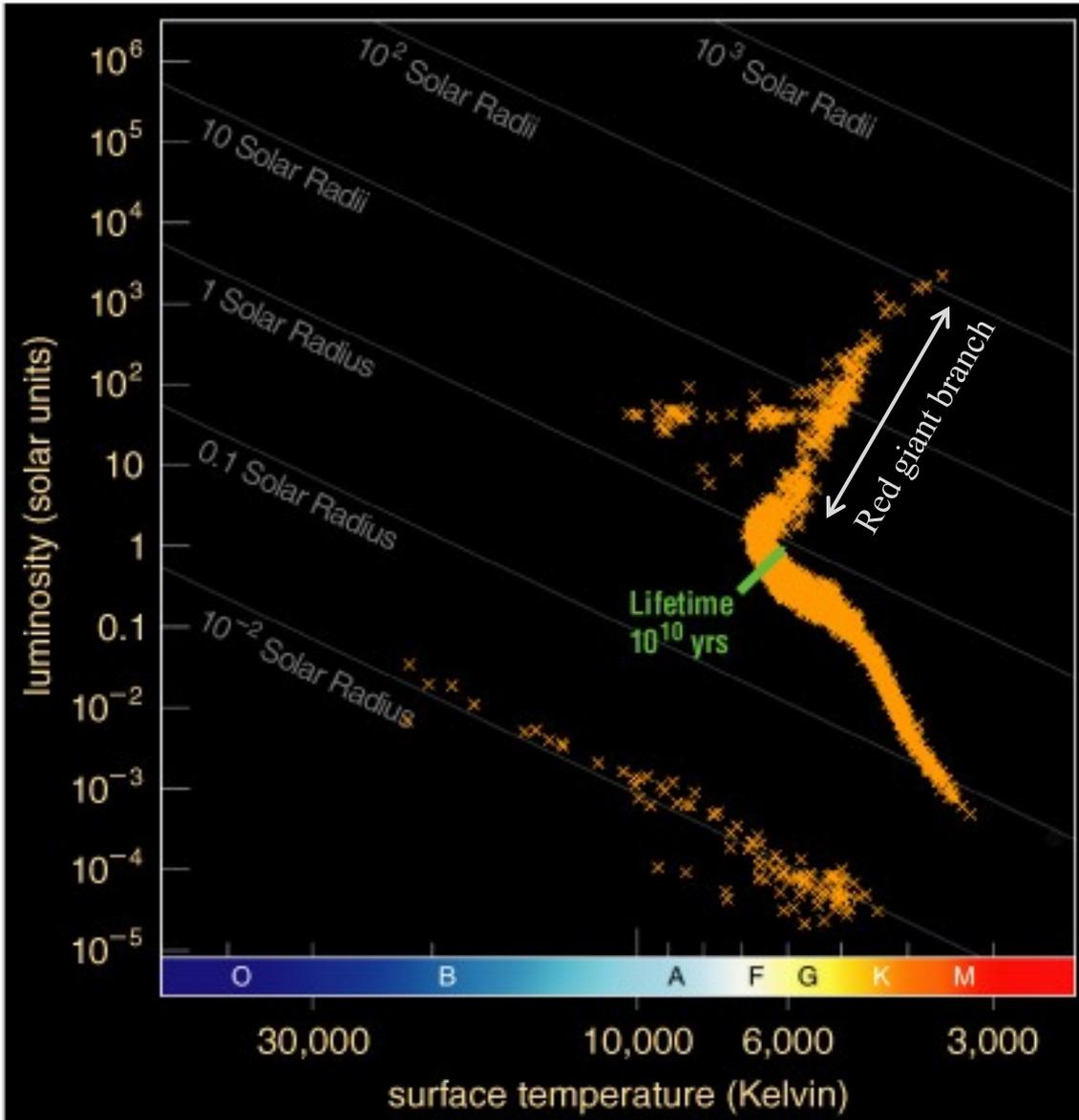
The turn-off point



To determine accurate ages, we compare models of stellar evolution to the cluster data.

Using the H-R Diagram to Determine the Age of a Star Cluster

The turn-off point



Detailed modeling of the oldest **globular clusters** reveals that they are about 13 billion years old.

Think/Pair/Share

Why do astronomers use the HR diagram so extensively?

- A. By plotting radius vs. core temperature, they can understand stellar properties and composition
- B. By plotting luminosity vs. surface temperature they can understand stellar types and evolution
- C. By plotting mass vs. luminosity, they can understand stellar formation and ages
- D. By plotting core temperature vs. luminosity they can understand stellar composition and evolution

Think/Pair/Share

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What have we learned?

Begin 3 minute review

What have we learned?

What are the two types of star clusters?

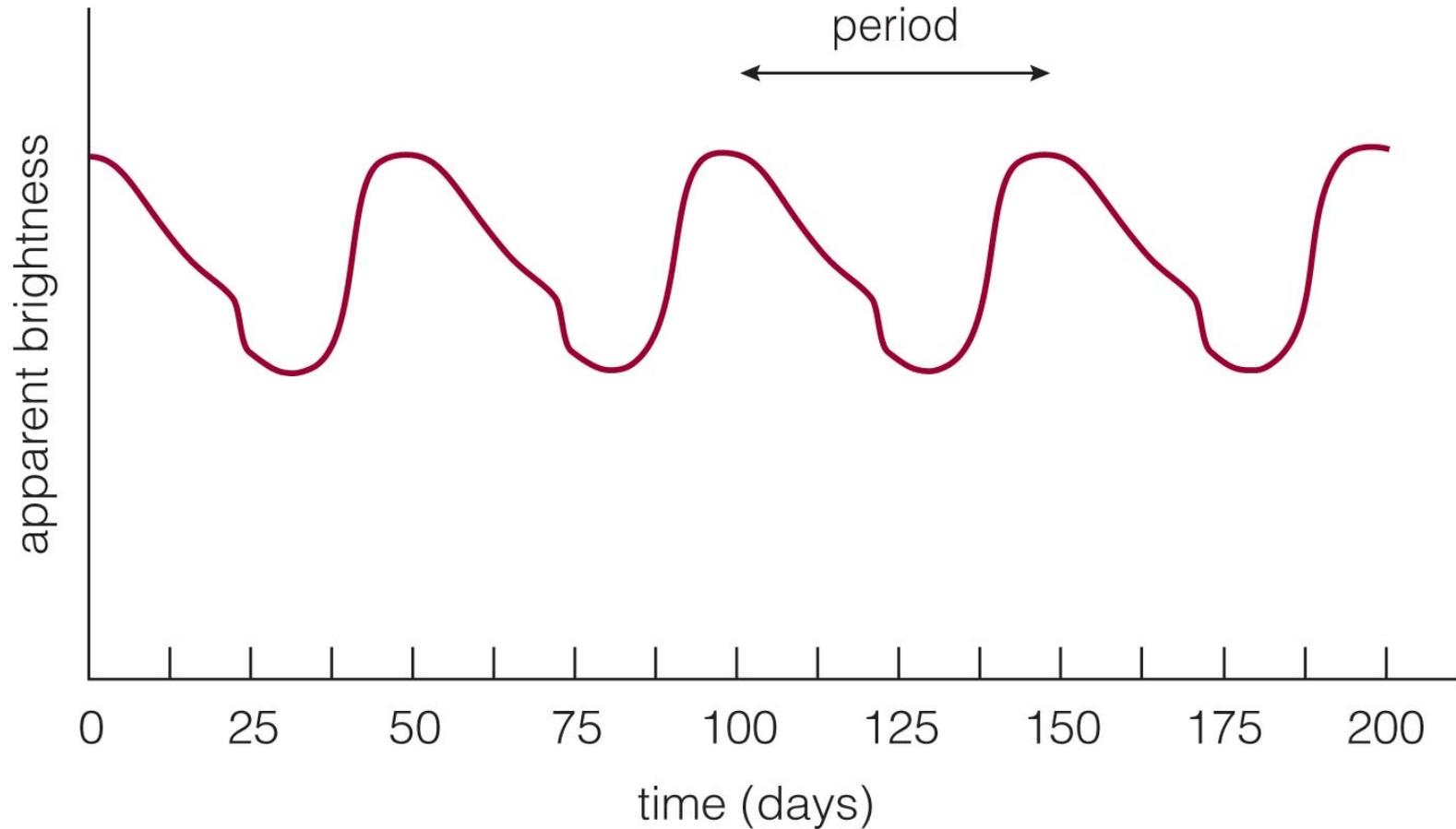
Open clusters are loosely packed and contain up to a few thousand stars.

Globular clusters are densely packed and contain hundreds of thousands of stars.

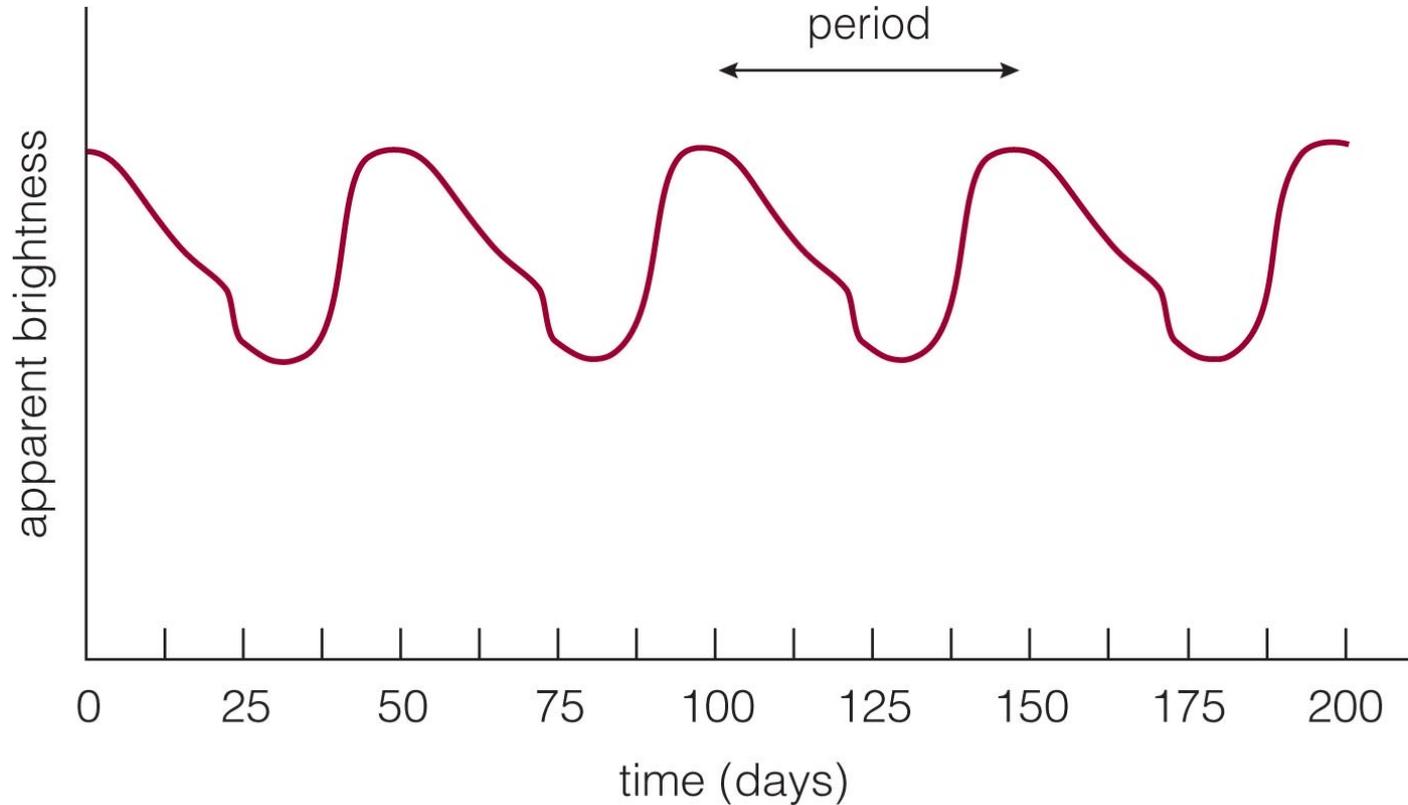
How do we measure the age of a star cluster?

A star cluster's age equals the life expectancy of its most massive stars still on the main sequence.

Why do the properties of some stars vary?



Pulsating Variable Stars

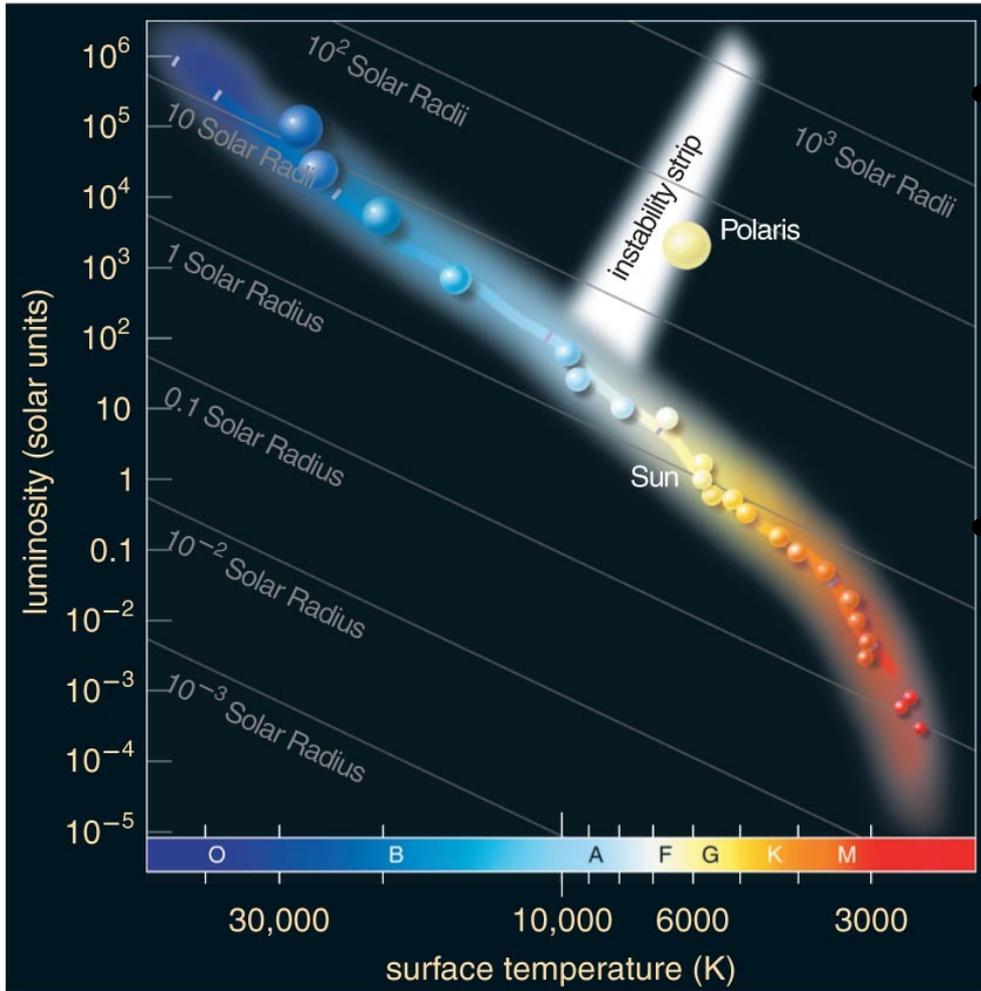


- The light curve of this *pulsating variable star* shows that its brightness alternately rises and falls over a 50-day period.

Variable Stars

- Any star that varies significantly in brightness with time is called a *variable star*.
- Some stars vary in brightness because they cannot achieve proper balance between power radiating coming from the core and power radiated from the surface.
- Such a star alternately expands and contracts, varying in brightness as it tries to find a balance.

Cepheid Variable Stars



Most pulsating variable stars inhabit an *instability strip* on the H-R diagram.

The most luminous ones are known as *Cepheid variables*.